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## Tri-op redactable blockchains with block modification, removal, and insertion

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**Abstract:** In distributed computations and cryptography, it is desirable to record events on a public ledger, such that later alterations are computationally infeasible. An implementation of this idea is called *blockchain*, which is a distributed protocol that allows the creation of an immutable ledger. While such an idea is very appealing, the ledger may be contaminated with incorrect, illegal, or even dangerous data, and everyone running the blockchain protocol has no option but to store and propagate the unwanted data. The ledger is bloated over time, and it is not possible to remove redundant information. Finally, missing data cannot be inserted later. *Redactable* blockchains were invented to allow the ledger to be mutated in a controlled manner. To date, redactable blockchains support at most two types of redactions: block modification and removal. The next logical step is to support block insertions. However, we show that this seemingly innocuous enhancement renders all previous constructs insecure. We put forward a model for blockchains supporting all three redaction operations and construct a blockchain that is provably secure under this formal definition.

**Key words:** Bitcoin, blockchain, redactable blockchain, block change, block insertion, block removal

### 1. Introduction

A traditional problem in distributed computing and cryptography is joint agreement: A set of parties wants to reach an agreement (consensus) over a noisy channel, while some parties may cooperate and deliberately act maliciously [1]. Nakamoto [2] proposed a solution in the context of cryptocurrencies, called *Bitcoin*. The goal was a decentralized digital currency, where the peers jointly agree on performing financial transactions and register them in a distributed ledger. Since the transactions were grouped to form blocks and blocks were chained together, the protocol is called the *blockchain*. Blockchain provides a mechanism to append any data type to the ledger. It can be seen as a protocol to agree on events jointly and register them irrevocably on a distributed ledger.

In general, a blockchain can be permissionless or permissioned [3]. Bitcoin is permissionless, as the parties do not need authentication to join the protocol. Permissioned blockchains, on the other hand, require a party to authenticate first before being able to take part in the protocol. The latter is quite common in exclusive environments, such as corporate applications (e.g., [4]). Due to the identifiability of parties and the possibility of removing the malicious ones, permissioned blockchains can simplify assumptions to achieve higher performance. However, they are not viable in environments without central trust.

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Regardless of the permission model of a blockchain, several researchers noted some issues with its immutability: The ledger can record unwanted data (including child pornography<sup>1</sup> or malware<sup>2</sup>). Therefore, participants have no choice but to save and propagate the unwanted data. In some jurisdictions, the propagator of such illegal content is considered complicit [5]. However, the participants cannot remove the unlawful content or stop propagating it with an immutable ledger. Another possible issue with immutability is the lack of privacy. Once private information is recorded in an immutable ledger, there is no way to remove it. Therefore, immutable blockchains cannot observe the “right to be forgotten” endowed to users by privacy laws such as the EU General Data Protection Regulation (GDPR). Protocol or implementation flaws pose another threat to immutability. In one famous case, the Ethereum cryptocurrency had an implementation flaw that made the DAO Attack<sup>3</sup> possible. As a result, malicious transactions were recorded in the immutable ledger of Ethereum. The only viable solution was for the majority of participants to upgrade their software. The new software resolved the flaw, effectively invalidating the malicious transactions. This solution is called a *hard fork*, and it is the last line of defense against such influential attacks on immutable blockchains. Immutability has other drawbacks: The size of the ledger increases over time and storing and processing it becomes increasingly resource-intensive. There is no possibility to reduce the size of the ledger by removing redundant information from it. Furthermore, there is no option to insert a block within the ledger, even if the participants later note that a block is mistakenly not registered (due to protocol issues, implementation mistakes, or oversight).

For these reasons, some researchers proposed the concept of *redactable* blockchains. A redactable blockchain allows the ledger to be controllably mutated once the need arises. In [8], two types of redactable blockchains were identified: (1) **Moderated**: In protocols of this type [6–9], a centralized authority (one or more administrators) has a secret redaction key. Once a redaction request is approved, it performs the required changes to the ledger using the secret key. The changes can be verified by all participants using the associated public key. (2) **Unmoderated**: In protocols of this type [10, 11], the parties vote on redaction requests. Once a certain quorum of votes is attained, the redaction is applied. The votes are added to the ledger as evidence.

A critical remark is distinguishing these concepts with permissioned or permissionless blockchains, as moderation has nothing to do with user authentication. Moderation authority only controls the redaction operations; it has nothing to do with permitting who can join the system. A blockchain can be both permissioned and moderated. Still, even in that case, it is possible to have two sets of authorities: one for authorizing users to join the blockchain and one for authorizing the redactions. We opted for the *moderated* setting in this work, since there are some serious attacks [8, 11] against the existing unmoderated protocols.

**Contributions.** We propose the first model and security definition for redactable blockchains that support three redaction operations: block change (**chg**), block insertion (**ins**), and block removal (**rem**). All previous redactable blockchains supported block change. Removal is previously used in one work [6] to shrink the ledger. To the best of our knowledge, we initiate the support for block insertion. Interestingly, we show that naively incorporating the seemingly innocuous insert operation renders the previous constructs insecure. We demonstrate this by what we call a “twin-block attack” on [6, 7, 9], and a “change-of-operation attack” on [8]. We then create a secure construct, and prove its security under our improved model. The construct alleviates all

<sup>1</sup>Hargreaves S, Cowley S. (2013). How porn links and Ben Bernanke snuck into Bitcoin’s code [online]. Website <https://tinyurl.com/bitcoin-snuck> [accessed 19 April 2021].

<sup>2</sup>Pearson, J. (2015). The Bitcoin blockchain could be used to spread malware, INTERPOL Says [online]. Website <https://tinyurl.com/bitcoin-malware> [accessed 2021 Apr 19].

<sup>3</sup>CoinDesk (2016). Understanding the DAO attack [online]. Website <https://tinyurl.com/dao-attack> [accessed 19 April 2021].

previous issues by introducing the concept of *triple versioning*, where each block holds three types of “versions”: A globally unique version number, the type of operation based on which the block is created, and the intended index of the block. Our construct uses a single digital signature per redaction, and is thus very efficient. Furthermore, it does not require any nonstandard assumptions.

## 2. Background

### 2.1. Related work in the moderated setting

The concept of redactable blockchains was pioneered by Ateniese et al. [6]. Their main idea was to construct a protocol on top of Bitcoin, and therefore had to cope with the limitations posed by Bitcoin. The resulting construct was therefore complicated: They introduced a primitive called *enhanced chameleon hash function*, in which collisions are hard to find except for an entity owning a secret key. The suggested construction of such hash functions required nonstandard assumptions and a large redaction witness (e.g., under the DLIN assumption, it required 39 group elements). Derler et al. [7] show how this idea can be further fine tuned to make the primitive policy based: Any entity that has enough privileges to satisfy a policy can find collisions. The idea is implemented by incorporating another primitive called a *ciphertext-policy attribute-based encryption*.

Grigoriev and Shpilrain [9] suggested a simple and efficient solution based on RSA, but their construct is insecure [8]. Dousti and Küpçü [8] provided another simple solution based on any strongly unforgeable digital signature. The efficiency of their protocol is a result of completely departing from Bitcoin, and not being restricted to its data structures and verification algorithms.

Except for [6], all previous work [7–11] (both moderated and unmoderated) support only one type of redaction: Changing blocks. In [6], the authors show how block removals can be supported as well. Attacks against various types of redactable blockchains are presented in [8, 11].

### 2.2. Preliminaries

**Notation.** Deterministic assignments are denoted by  $z := 9$ , while probabilistic assignments are denoted by an arrow:  $z \leftarrow B(n)$  for the output of a probabilistic algorithm  $B$ , or  $z \leftarrow S$  for uniformly random selection from a finite set  $S$ . The symbol  $x = y$  is used for checking/asserting equality. Let  $\mathcal{L} = [B_0, \dots, B_\ell]$  be a list. Note that we use 0 and  $\ell$  as the indices of the first and the last element of the list, respectively. The list may grow arbitrarily, but  $\ell$  is always updated accordingly to be the index of the last element. The elements of the list can be addressed by their index:  $\mathcal{L}[i] = B_i$  for  $0 \leq i \leq \ell$ . For integers  $i, j$  with  $0 \leq i \leq j \leq \ell$ , define  $\mathcal{L}[i : j] \stackrel{\text{def}}{=} [B_i, \dots, B_j]$ . If  $j < i$ , then  $\mathcal{L}[i : j] = []$  by definition. If  $\mathcal{L}_1$  and  $\mathcal{L}_2$  are two lists, their concatenation is denoted by  $\mathcal{L}_1 + \mathcal{L}_2$ . A function  $\text{negl}: \mathbb{N} \rightarrow [0, 1]$  is called negligible if it decays faster than the inverse of any positive polynomial. Formally, for any  $c \in \mathbb{N}$ , there exists  $n_0 \in \mathbb{N}$ , such that for all integers  $n > n_0$  we have  $\text{negl}(n) < n^{-c}$ .

**Definition 1 (Strongly unforgeable signature scheme)** Consider a signature scheme  $(\text{GenSig}, \text{Sign}, \text{VerifySig})$  where  $\text{GenSig}$  generates a pair of public and secret keys,  $\text{Sign}$  generates a signature given the secret key and a message, and  $\text{VerifySig}$  verifies a signature on some message using the public key. The signature scheme is called strongly unforgeable under chosen-message attack (*sUF-CMA*), if for any efficient adversary taking part in the following game, there exists a negligible function  $\text{negl}$ , such that the probability of the adversary winning is at most  $\text{negl}(\lambda)$ , where  $\lambda$  is the security parameter.

- $\text{GenSig}(1^\lambda)$  generates a pair of public and secret keys  $(pk, sk)$ .
- The adversary is given  $pk$ , as well as access to the signing oracle  $\text{Sign}_{sk}(\cdot)$ . The signing oracle receives a message, and returns a valid signature on it. The adversary may interact with the oracle polynomially many times.
- The adversary outputs a pair  $(m^*, \sigma^*)$ . She is said to win the game if  $\text{VerifySig}(pk, m^*, \sigma^*) = 1$ , and  $\sigma^*$  is never returned by the signing oracle on input  $m^*$ .

Our construction assumes the existence of sUF-CMA signature schemes. The assumption is equivalent to the existence of ordinary (i.e. not necessarily strong) UF-CMA signature schemes [12], which can be constructed from one-way functions [13]. However, very efficient constructs of sUF-CMA signature schemes exist [14, p. 230].

### 3. Blockchain operations

This section illustrates the ways a ledger can be modified using diagrams in Figure 1. To this end, let us first fix the block structure. The most important part of a block is the block content  $C$ . Blocks must also contain a witness  $W$  supporting the validity of redactions. Other information, such as block prefix, version number, randomness and so on are immaterial to the discussion of this section. We simply use an ellipsis ( $\dots$ ) to show the omission of such extra information.

The first type of blockchain operation is *appending* a block. It does not require access to the secret key. Here, we define the *pivot block* as the block being appended. All other operations that can be performed on the ledger are redactions. They require access to the secret key. For each redaction operation, we define one block as the *pivot block*: It is the block for which a new witness is computed (using the secret key). The specifics for each operation is explained next:

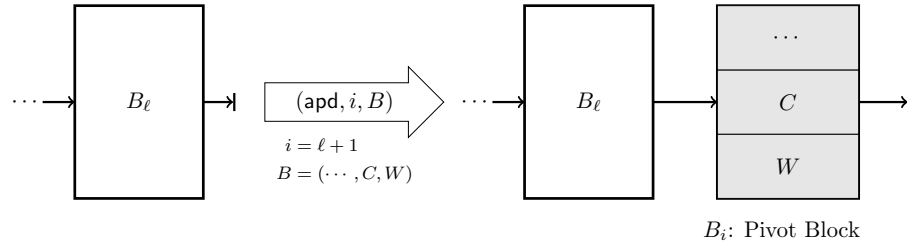
**Append operation  $\text{apd}$  (Figure 1a):** Consider the appending request  $(\text{apd}, i, B)$ , asking to append the block  $B$  at location  $i$ . When the last block of the ledger is at location  $\ell$ , the operation is only successful for  $i = \ell + 1$ . Here, the *pivot block* is the block being appended ( $B$ ).

**Change operation  $\text{chg}$  (Figure 1b):** Consider the redaction request  $(\text{chg}, i, C')$ , asking to change the content of the  $i^{\text{th}}$  block to  $C'$ . Here, the *pivot block* is the block being changed (the  $i^{\text{th}}$  block). The administrator uses the secret key  $sk$  to find a proper witness  $W'_i$  so that the redaction is valid.

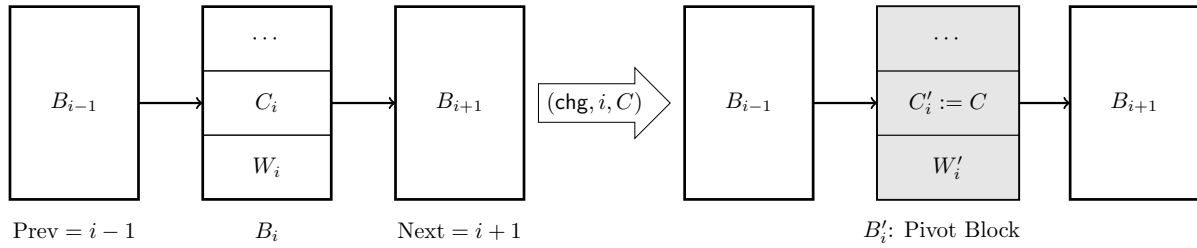
**Insertion operation  $\text{ins}$  (Figure 1c):** Consider the redaction request  $(\text{ins}, i, C')$ , asking to insert a block with content  $C'$  at index  $i$ . Here, the *pivot block* is the block being inserted (the  $i^{\text{th}}$  block). The administrator uses the secret key  $sk$  to find a proper witness  $W'_i$ .

**Removal operation  $\text{rem}$  (Figure 1d):** Consider the redaction request  $(\text{rem}, i)$ , asking to remove the block at index  $i$ . Here, the *pivot block* is the block preceding the block being removed (the block with index  $i - 1$ ). The administrator uses the secret key  $sk$  to find a proper witness  $W'_{i-1}$ .

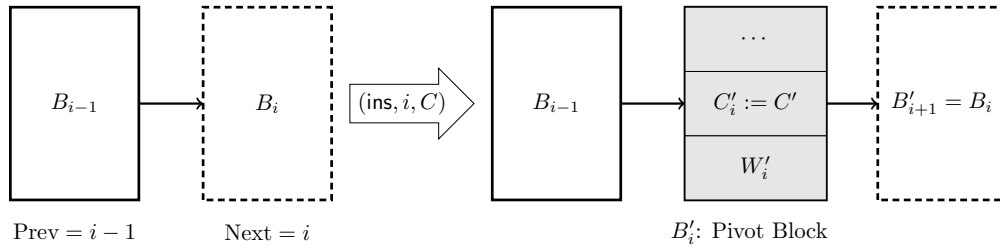
Table 1 summarizes the operations, as well as utility functions  $\text{Ind}$ ,  $\text{Prev}$ ,  $\text{Next}$ , and  $\text{Pivot}$ . These utility functions are used in later sections of the paper to simplify definitions.  $\text{Ind}$  gives the set of valid indices for an



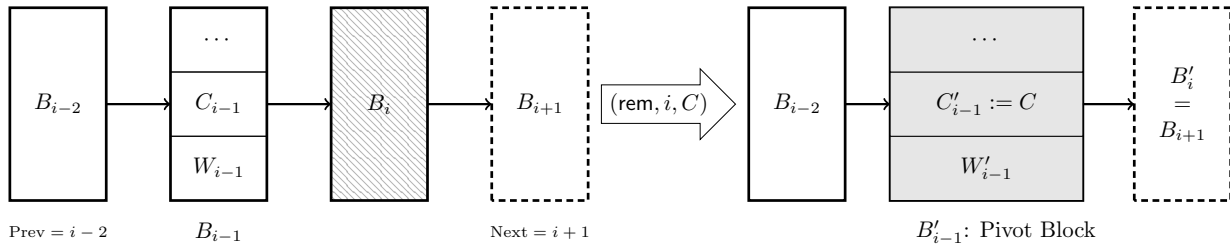
(a) Append operation (**apd**,  $i, B$ ). The pivot block is the one being appended.



(b) Redaction operation (**chg**,  $i, C$ ). The pivot block is the one being changed.



(c) Redaction operation (**ins**,  $i, C$ ). The pivot block is the one being inserted.



(d) Redaction operation (**rem**,  $i, C$ ). The pivot block is the one preceding the block being removed.

**Figure 1.** Illustration of various block redaction operations. The grayed fields of the pivot block are affected by the corresponding operation.

operation. Pivot returns the index of the pivot block for each operation, while Prev and Next return the index of the previous and next blocks. Notice that all indices refer to the locations in the ledger prior to performing the operation.

**Table 1.** Various operations for a redactable blockchain.  $\text{Ind}_\ell(\text{op})$  denotes the set of valid indices  $i$  for operation  $\text{op}$  on a ledger whose last index is  $\ell$ . For each operation, previous and next indices are listed. Note that they refer to block indices in the ledger *prior* to performing the operation.

| Operation | Name   | Redaction? | $\text{Ind}_\ell(\text{op})$ | $\text{Prev}(\text{op}, i)$ | $\text{Next}(\text{op}, i)$ | $\text{Pivot}(\text{op}, i)$ |
|-----------|--------|------------|------------------------------|-----------------------------|-----------------------------|------------------------------|
| apd       | Append | □          | $\{\ell + 1\}$               | $i - 1$                     | $i + 1$                     | $i$                          |
| chg       | Change | ⊗          | $\{1, \dots, \ell\}$         | $i - 1$                     | $i + 1$                     | $i$                          |
| ins       | Insert | ⊗          | $\{1, \dots, \ell\}$         | $i - 1$                     | $i$                         | $i$                          |
| rem       | Remove | ⊗          | $\{1, \dots, \ell\}$         | $i - 2$                     | $i + 1$                     | $i - 1$                      |

#### 4. The tri-op model

Our model augments that of [8] with two types of new redactions: Block removal and block insertion. The model is described as a game between a challenger and an adversary. The challenger generates a pair of keys and initializes the ledger. The public key is handed over to the adversary. She also receives read-only access to the ledger, as well as oracle access to the challenger. The adversary can make two types of queries to the challenger:

1. **Installation query:** The adversary asks the challenger to install a block at a specific location in the ledger while performing one of the four types of operations (append, change, remove, or insert). The challenger verifies the request and performs it in case it is valid.
2. **Redaction query:** The adversary asks the challenger to redact a block using one of three redaction operations (change, remove, or insert). The challenger verifies the request. If the operation is valid, the challenger uses the secret key to perform the operation and returns a block that can later be installed by the adversary in the ledger using an installation query.

This model abstracts out the distributed nature of a blockchain. As a result, it does not capture all real-world attacks. For instance, the adversary does not get the option to change multiple blocks at once. Therefore, as shown in the next section, the constructs need not worry about chaining the blocks together. In some sense, it is an ideal-world model of redactions. When used with real-world constructs, it should somehow be composed with a blockchain model that captures attacks against ordinary blockchains. Our model is simple enough and is suitable for proof-reading constructs against nondistributed attacks. In Section 7, we discuss possible extensions to capture a distributed model.

We next provide a definition of tri-op redactable blockchains, which as the name suggests, support three types of redaction operations. The definition uses the following useful function:

$$\text{Transform}(\mathcal{L}, (\text{op}, i, B)) \stackrel{\text{def}}{=} \mathcal{L}[0 : \text{Prev}(\text{op}, i)] + [B] + \mathcal{L}[\text{Next}(\text{op}, i) : \ell] \quad (1)$$

It defines the transformation performed on ledger  $\mathcal{L}$  when performing an installation of block  $B$  at location  $i$  using operation  $\text{op} \in \{\text{apd}, \text{chg}, \text{rem}, \text{ins}\}$ . It is assumed that  $i \in \text{Ind}_\ell(\text{op})$ , as otherwise it will be rejected.

**Definition 2** A quintuple of efficient algorithms  $3\mathcal{RBC} = (\text{Gen}, \text{Create}, \text{Redact}, \text{Verify}, \text{Install})$  is called a tri-op redactable blockchain scheme if:

1. Algorithm **Gen** takes the security parameter  $1^\lambda$  in unary and generates a pair of public and private keys  $(pk, sk)$ , along with the initialized ledger  $\mathcal{L}$ .

2. Algorithm **Create** creates a new block  $B$ , when executed on input the public key  $pk$ , the ledger  $\mathcal{L}$ , and some block content  $C$ .
3. Algorithm **Redact** generates a redacted block using the secret key. More specifically,  $\text{Redact}(sk, \mathcal{L}, (\text{op}, i, C))$  outputs a redacted block  $B$  for operation  $\text{op} \in \{\text{chg}, \text{ins}, \text{rem}\}$  at index  $i$  of ledger  $\mathcal{L}$ , where  $sk$  is the secret key and  $C$  is some block content.
4. Algorithm **Verify** verifies the validity of an operation on the ledger. More specifically, let  $(\text{op}, i, B)$  denote putting block  $B$  at index  $i$  of the ledger by performing operation  $\text{op} \in \{\text{apd}, \text{chg}, \text{ins}, \text{rem}\}$ . Then,  $\text{Verify}(pk, \mathcal{L}, (\text{op}, i, B))$  returns 1 if and only if this operation is valid.

We observed that splitting the verification algorithm into two separate checks makes it much more flexible, as one part can be independent of the history of ledger transforms: The first part (algorithm  $\Phi$ ) verifies whether the operation is valid on the current ledger. The second part (algorithm  $\Psi$ ) verifies whether the (resulting) ledger is valid, regardless of the operation. For the first part, the blockchain designer should decide what part of each block is involved in the verification. We call that part the “version of the (pivot) block”:

$$V := \text{Version}(\mathcal{L}[\text{Pivot}(\text{op}, i)]). \quad (2)$$

We also extract the version of all existing blocks in the ledger prior to the operation:

$$\vec{V} := [\text{Version}(\mathcal{L}[0]), \dots, \text{Version}(\mathcal{L}[\ell])]. \quad (3)$$

Algorithm  $\Phi$  then compares the new version information against the existing ones, when  $\text{op}$  is the operation and  $i$  is the index:  $\Phi(\vec{V}, \text{op}, i, V)$ . It returns 1 if and only if the operation is deemed valid.

The second algorithm  $\Psi(pk, \mathcal{L}^*)$  checks the consistency of the whole ledger assuming the transformation is done:

$$\mathcal{L}^* := \text{Transform}(\mathcal{L}, (\text{op}, i, B)). \quad (4)$$

In one sense,  $\Psi$  performs a static check on the ledger, while  $\Phi$  performs a dynamic check on the operation. The verification algorithm returns 1 if and only if both  $\Phi(\vec{V}, \text{op}, i, V)$  and  $\Psi(pk, \mathcal{L}^*)$  return 1.

5. Algorithm **Install** modifies the ledger according to the requested operation. More specifically, when executed as  $\text{Install}(pk, \mathcal{L}, (\text{op}, i, B))$ , the algorithm first performs  $\text{Verify}(pk, \mathcal{L}, i, B)$ , and returns 0 if the verification fails. Otherwise, it performs  $\mathcal{L} = \text{Transform}(\mathcal{L}, (\text{op}, i, B))$ , and returns 1.

Any tri-op redactable blockchain  $3\mathcal{RBC}$  should be correct, meaning that when the algorithms **Create** and **Redact** are executed on valid inputs, their output must satisfy the verification algorithm:

**Definition 3** Let  $\lambda$  be any security parameter, and  $3\mathcal{RBC} = (\text{Gen}, \text{Create}, \text{Redact}, \text{Verify}, \text{Install})$  be as in Definition 2. Let  $(pk, sk, \mathcal{L}) \leftarrow \text{Gen}(1^\lambda)$ , and assume that  $\mathcal{L}$  is transformed any number of times by applying the **Install** algorithm. The following correctness conditions should hold:

1. **Algorithm Create is correct:** Let  $B$  be generated by  $\text{Create}(pk, \mathcal{L}, C)$ . Then

$$\text{Content}(B) = C \quad \wedge \quad \text{Verify}(pk, \mathcal{L}, (\text{apd}, \ell + 1, B)) = 1. \quad (5)$$



1. Let  $(pk, sk, \mathcal{L}) \leftarrow \text{Gen}(1^\lambda)$ . The set of query-responses  $\text{Hist}$  is initialized to the empty set  $\emptyset$ .
2. Adversary  $\mathcal{A}$  is given  $pk$  and a read-only access to the ledger  $\mathcal{L}$ . She can query two oracles  $\text{REDC}_{sk, \mathcal{L}}(\cdot, \cdot, \cdot)$  and  $\text{INST}_{pk, \mathcal{L}}(\cdot, \cdot, \cdot)$ , which operate as explained below.
3. Upon receiving  $(\text{op}, i, C)$  where  $\text{op} \in \{\text{chg}, \text{ins}, \text{rem}\}$ , the redaction oracle  $\text{REDC}$  generates  $B$  by running  $\text{Redact}(sk, \mathcal{L}, (\text{op}, i, C))$ . If  $B \neq \perp$ , it adds  $(\text{op}, i, B)$  to  $\text{Hist}$ . Finally  $B$  is returned.
4. Upon receiving  $(\text{op}, i, B)$ , the installation oracle  $\text{INST}$  executes  $\text{Install}(pk, \mathcal{L}, (\text{op}, i, B))$ . Let  $b$  be the output of the installation algorithm. If  $b = 0$ , the experiment ends by returning 0. Otherwise,
  - **If:**  $\text{op} \neq \text{apd}$  and  $(\text{op}, i, B) \notin \text{Hist}$ : The adversary  $\mathcal{A}$  succeeds. The experiment ends by returning 1.
  - **Else:** In case  $(\text{op}, i, B) \in \text{Hist}$ , the installation oracle sets  $\text{Hist} := \emptyset$ . The adversary receives 1, and the experiment continues.

**Experiment.** The redaction experiment  $\text{Redact}_{\mathcal{A}, 3\mathcal{RBC}}(\lambda)$ .

2. **Algorithm Redact is correct:** For any  $\text{op} \in \{\text{chg}, \text{ins}, \text{rem}\}$  and  $i \in \text{Ind}_\ell(\text{op})$ , let  $B$  be generated by  $\text{Redact}(sk, \mathcal{L}, (\text{op}, i, C))$ . Then

$$\text{Content}(B) = C \quad \wedge \quad \text{Verify}(pk, \mathcal{L}, (\text{op}, i, B)) = 1. \quad (6)$$

We can now give the security definition for a tri-op redactable blockchain, which is based on Section 4. The experiment uses a set  $\text{Hist}$  to keep track of queries made to the redaction oracle: when a valid query  $(\text{op}, i, C)$  is made to this oracle and a block  $B$  is returned as a response, the element  $(\text{op}, i, B)$  is added to  $\text{Hist}$ . The adversary wins if she performs a valid install query for a redacted block not in  $\text{Hist}$ .

It is noteworthy that once a valid installation query is processed, the experiment empties the set  $\text{Hist}$ . This provides the adversary with a great opportunity: she can win even if she can get two redacted blocks from the administrator, and install both of them. In other words, for a secure  $3\mathcal{RBC}$ , once a redacted block is installed, all previously obtained redacted blocks must be rendered invalid.

The above definition is very strict. Alternatively, we could have kept all previously obtained blocks in  $\text{Hist}$  to relax the definition. However, since the insertion and removal of blocks relocate all succeeding blocks, the index  $i$  in corresponding elements of  $\text{Hist}$  must be readjusted: a block insertion should add 1 to the index of triplets in  $\text{Hist}$ , whose index is after the installation location. Similarly, a block removal should subtract 1 from those indices. While the relaxation in security definition is perceivable, we did not incorporate it in Section 4, as otherwise, it would unnecessarily complicate the experiment. Surprisingly, this stricter model simplified our construction and security proof (next section) compared to the alternative.

**Definition 4** A tri-op redactable blockchain scheme  $3\mathcal{RBC}$  is secure if for all efficient adversaries  $\mathcal{A}$  who takes part in Section 4, there exists a negligible function  $\text{negl}$  such that  $\Pr[\text{Redact}_{\mathcal{A}, 3\mathcal{RBC}}(\lambda) = 1] \leq \text{negl}(\lambda)$ .

## 5. Attacks on previous work

In this section, we show how adding support for block insertion renders previous moderated blockchains insecure. Most previous constructs succumb to what we call a “twin-block attack” (Section 5.1), while one construct is susceptible to a “change-of-operation attack” (Section 5.2).

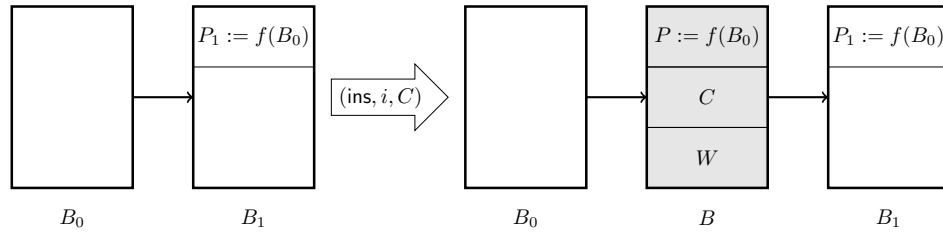
### 5.1. Twin-block attack

Most of the previous redactable blockchains in the moderated setting [6, 7, 9] follow the following structure: Blocks contain a prefix  $P$ , some content  $C$ , and a witness  $W$ . The witness is computed by the administrator when redacting a block. The prefix of a block is computed as a function of the previous block:  $P_{i+1} := f(B_i)$ , where  $f$  is some deterministic function.

Once insertion is recognized as an operation, the deterministic nature of  $f$  becomes an issue: when a block is inserted between two blocks, its prefix equals to that of the next block: see Figure 2, and read on for a formal proof. We refer to two consecutive blocks with the same prefixes as *twin blocks*. Next, it is shown how the adversary can create and exploit such blocks to make some arbitrary modifications to the ledger, without consulting the administrator first.

Consider a “toy” ledger  $\mathcal{L} = [B_0, B_1]$ . By definition,  $P_1$  is a deterministic function of the previous block:

$$P_1 := f(B_0). \quad (7)$$



**Figure 2.** Illustration of how twin blocks are created.

**Two-step setup:** The adversary  $\mathcal{A}$  performs the following:

1.  $\mathcal{A}$  queries `Redact` on  $(ins, 1, C)$ , and receives block  $B = (P, C, W)$ . In particular,  $W$  is set in such a way that the prefix of the next block  $B_1$  remains valid: in the context of enhanced chameleon hash functions introduced in Section 2.1, the administrator uses its secret key to find  $W$  such that  $B$  and  $B_0$  form a collision for  $f$ .
2.  $\mathcal{A}$  queries `Install` on  $(ins, 1, B)$ . The resulting ledger is  $\mathcal{L} = [B_0, B, B_1]$ .

The following identities hold in the ledger:

$$P = f(B_0), \quad (8)$$

$$P_1 = f(B). \quad (9)$$

Equation (8) holds since  $B$  is a valid next block of  $B_0$ , and Equation (9) holds because  $B_1$  is a valid next block of  $B$ . Together with Equation (7) we get:

$$P = P_1 = f(B_0) = f(B). \quad (10)$$

**Attack 1:** Without any other `Redact` queries, adversary can ask `Install` on  $(ins, 1, B)$ , resulting in the valid ledger  $\mathcal{L} = [B_0, B, B, B_1]$ . The ledger is valid because  $B$  is a valid next block of  $B_0$  (as was the case before), and  $B$  is a valid next block of itself:  $P = f(B)$  as per Equation (10). Therefore, the adversary can insert  $B$  in the ledger indefinitely by querying `Install` on  $(ins, 1, B)$  an arbitrary number of times.

**Attack 2:** Starting with  $\mathcal{L} = [B_0, B, B, B_1]$  obtained in the previous attack,  $\mathcal{A}$  can ask the redaction oracle to change the block  $B$  at index 1, but apply it to its “twin block”  $B$  at index 2:

1.  $\mathcal{A}$  queries **Redact** on  $(\text{chg}, 1, \tilde{C})$ , and receives block  $\tilde{B} = (\tilde{P}, \tilde{C}, \tilde{W})$ , satisfying the following identities:

$$\tilde{P} = f(B_0), \quad P = f(\tilde{B}). \quad (11)$$

2.  $\mathcal{A}$  queries **Install** on  $(\text{chg}, 2, \tilde{B})$ , resulting in the valid ledger  $\mathcal{L} = [B_0, B, \tilde{B}, B_1]$ . This is because combining Equations (10) and (11), we get:

$$\tilde{P} = f(B), \quad P_1 = f(\tilde{B}). \quad (12)$$

Therefore  $\tilde{B}$  is a valid next block of  $B$ , and  $B_1$  is a valid next block of  $\tilde{B}$ .

## 5.2. Change-of-operation attack

The construct of [8] has the block structure  $B = (C, V, W)$ , where  $C$  is the block content,  $V$  is the block version number, and  $W$  is a witness to be provided whenever a block is redacted. Notice that blocks do not have a prefix, as the model is abstract, and chaining blocks occurs at a lower level.

- The versioning scheme is global, meaning that each block will have a unique version number. In other words, with each installation (be it an append or a redaction), a new version number is introduced.
- The witness for a nonredacted block is the empty string  $\varepsilon$ . Once a block is redacted, the witness becomes a digital signature on a value specified below. The signing secret key is only known to the administrator.

Let  $\mathcal{L} = [(C_1, 1, \varepsilon), (C_2, 2, \varepsilon), (C_3, 3, \varepsilon)]$  be the current ledger, and assume we want to append a block whose content is  $C_4$ . The version number of this block must be unique in the ledger, so we set it to 4. The witness is set to the empty string. Therefore, the fourth block is  $B_4 = (C_4, 4, \varepsilon)$ , and the updated ledger becomes  $\mathcal{L} = [(C_1, 1, \varepsilon), (C_2, 2, \varepsilon), (C_3, 3, \varepsilon), (C_4, 4, \varepsilon)]$ .

Now assume the administrator wants to approve a change to the second block so that its new content becomes  $C'_2$ . The new block must have a unique version in the ledger, so the version is set to 5. Finally, the witness of the redacted block must be set. The signature is computed on the concatenation of three items: (1) the content of the redacted block, (2) the version of the redacted block, and (3) the version of the next block. The first two components are there to ensure that the adversary does not change the block content or version after she received a signed redacted block from the administrator. The third component is there to prevent an adversary to relocate a signed redacted block (i.e. receive a redaction for location  $i$ , but later install it at location  $i'$ ). In our example, the current version of the redacted block is 5, and the version of the next block in the ledger is 3. Therefore,  $W'_2$  is the administrator’s signature on the following string:  $C'_2 \parallel 5 \parallel 3$ , and the ledger after installation of this block becomes  $\mathcal{L} = [(C_1, 1, \varepsilon), (C'_2, 5, W'_2), (C_3, 3, \varepsilon), (C_4, 4, \varepsilon)]$ .

Let us exemplify one last modification to our example ledger. To change the content of the third block to  $C'_3$ , its version is set to 6, and its witness  $W'_3$  is set to a signature on  $C'_3 \parallel 6 \parallel 4$ . The ledger is updated to  $\mathcal{L} = [(C_1, 1, \varepsilon), (C'_2, 5, W'_2), (C'_3, 6, W'_3), (C_4, 4, \varepsilon)]$ .

The issue here is that  $W'_2$  is no longer a valid signature since the version number on the next block is changed. The construct resolved this issue by defining a *conditional* signature checking algorithm: the signature

is only checked if the version of the current block is less than that of the next block (i.e. the next block is not changed after the current block). The algorithm  $\Psi$  is defined as the logical AND:  $\bigwedge_{i=1}^{\ell} \psi(pk, \mathcal{L}[i-1], \mathcal{L}[i])$ , where  $\psi$  is defined as follows for any two blocks  $B = (C, V, W)$  and  $B' = (C', V', W')$ :

$$\psi(pk, B, B') \stackrel{\text{def}}{=} \begin{cases} 1 & \text{if } V' > V, \\ \text{VerifySig}(pk, C \parallel V \parallel V', W) & \text{if } V' < V. \end{cases} \quad (13)$$

While the above construct is provably secure in the single-operation model, it suffers from a simple *change-of-operation* attack. Consider a toy example ledger  $\mathcal{L} = [(C_1, 1, \varepsilon), (C_2, 2, \varepsilon)]$ . The adversary requests the redaction  $(\text{chg}, 1, C'_1)$ , and receives the block  $B'_1 = (C'_1, 3, W'_1)$ , where  $W'_1$  is a signature on  $C'_1 \parallel 3 \parallel 2$ . However, instead of installing  $(\text{chg}, 1, B'_1)$ , the adversary requests to install  $(\text{ins}, 2, B'_1)$ . Notice that the requested operation is changed from **chg** to **ins**, and the location is changed from 1 to 2. If succeeds, the ledger will become  $\mathcal{L} = [(C_1, 1, \varepsilon), (C'_1, 3, W'_1), (C_2, 2, \varepsilon)]$ , while the administrator's approved redaction was  $\mathcal{L} = [(C'_1, 3, W'_1), (C_2, 2, \varepsilon)]$ .

The above attack succeeds because the construct checks two conditions: (1) the redacted block version is globally unique. In this case, the version is 3 and satisfies this condition. (2) the condition in Equation (13), which also passes:  $W'_1$  is a valid signature on its own block content and version, as well as the version of the next block.

The reason why the above attack works is that the construct does not readily generalize to the tri-op settings: the adversary can always request a redaction using one operation, and install it at the proper location with another operation. As the above example shows, the result can be catastrophic: the adversary can make structural changes to the ledger that are not approved by the administrator. In the next section, we make some changes and suggest a new construct that is provably secure under the tri-op model.

## 6. Construction

In this section, we construct a tri-op redactable blockchain (Section 6.1) based on the idea of triple versioning. We then prove its security (Section 6.2) according to our proposed model and security definition. We finalize with experimental evaluation (Section 6.3).

### 6.1. A secure construct based on triple versioning

For a secure tri-op redactable blockchain, we improve the construct described in Section 5.2. The idea is to change the block structure to carry extra information regarding the operation and location for which the block is generated. In Definition 2, the only part of the verification algorithm that has access to this information is  $\Phi(\vec{V}, \text{op}, i, V)$ . Therefore, the appropriate place to add the operation and location of the block is its version element. Accordingly, the version of each block becomes a triplet  $V = (V_{\text{me}}, V_{\text{op}}, V_{\text{idx}})$ , where:

- $V_{\text{me}}$  is the actual version of the current block, and should be globally unique.
- $V_{\text{op}} \in \{\text{apd}, \text{chg}, \text{ins}, \text{rem}\}$  is the operator for which the block is generated.
- $V_{\text{idx}}$  is the location for which the block is generated.

We then define the following verification algorithms ( $\vec{V}$  is as defined in Equation (3)):

$$\text{MaxV}(\vec{V}) \stackrel{\text{def}}{=} 1 + \max_{0 \leq i \leq \ell} \vec{V}_{\text{me}}[i], \quad (14)$$

$$\begin{aligned} \Phi(\vec{V}, \text{op}, i, V) \stackrel{\text{def}}{=} & (\text{op} \in \{\text{apd}, \text{chg}, \text{ins}, \text{rem}\}) \wedge (i \in \text{Ind}_{|\vec{V}|}(\text{op})) \\ & (V_{\text{op}} = \text{op}) \wedge (V_{\text{idx}} = i) \wedge (V_{\text{me}} = \text{MaxV}(\vec{V})), \end{aligned} \quad (15)$$

$$\psi(pk, B) \stackrel{\text{def}}{=} \begin{cases} 1 & \text{if } V_{\text{op}} = \text{apd}, \\ \text{VerifySig}(pk, C \parallel V, W) & \text{otherwise.} \end{cases}, \quad (16)$$

$$\Psi(pk, \mathcal{L}) \stackrel{\text{def}}{=} \bigwedge_{0 \leq i \leq \ell} \psi(pk, \mathcal{L}[i]). \quad (17)$$

Algorithm  $\text{MaxV}(\vec{V})$  finds the maximum  $V_{\text{me}}$  in the ledger and adds 1 to it. Algorithm  $\Phi$  ensures that the block being installed is valid: it has the proper operation, the location at which it is installed matches the operation, and its version triplet is correct. Algorithm  $\psi$  checks whether the block is installed using a redaction operation, and if so the witness  $W$  is a valid signature on  $C \parallel V$ . Finally,  $\Psi$  applies  $\psi$  to all blocks in the ledger and returns 1 if all of them return 1.

**Construct 1** Let  $3\mathcal{RBC}_{\text{tv}}$  be a tri-op redactable blockchain, defined as follows. Each block is structured as a triple  $B = (C, V, W)$ , where  $C$  is the block content,  $V$  is the block version and  $W$  is a redaction witness. The block version is a triplet  $V = (V_{\text{me}}, V_{\text{op}}, V_{\text{idx}})$ .

- $\text{Gen}(1^\lambda)$  calls the generator of some signature scheme to generate a key pair:  $(pk, sk) \leftarrow \text{GenSig}(1^\lambda)$ . It then initializes the ledger as list containing a single element  $B_0 := (\varepsilon, (1, \text{apd}, 0), \varepsilon)$ .
- $\text{Create}(pk, \mathcal{L}, C)$  generates  $B := (C, (V_{\text{me}}, \text{apd}, \ell + 1), \varepsilon)$ , where  $V_{\text{me}} = \text{MaxV}(\vec{V})$  as per Equation (14).
- $\text{Redact}(sk, \mathcal{L}, (\text{op}, i, C))$ : If  $\text{op} \notin \{\text{chg}, \text{ins}, \text{rem}\}$  or  $i \notin \text{Ind}_\ell(\text{op})$ , it returns  $\perp$ . Otherwise, it creates a block  $B := (C, V, W)$  using content  $C$ , where  $V = (V_{\text{me}}, V_{\text{op}}, V_{\text{idx}}) = (\text{MaxV}(\vec{V}), \text{op}, i)$  and:

$$W \leftarrow \text{Sign}_{sk}(C \parallel V). \quad (18)$$

- $\text{Verify}(pk, \mathcal{L}, (\text{op}, i, B))$ : Let algorithms  $\Phi$  and  $\Psi$  be as in Equation (15) and Equation (17), respectively. The verification algorithm sets  $\mathcal{L}^* := \text{Transform}(\mathcal{L}, (\text{op}, i, B))$ , executes  $\Phi(\vec{V}, \text{op}, i, V)$  and  $\Psi(pk, \mathcal{L}^*)$ , and returns 1 if and only if both return 1.
- $\text{Install}(pk, \mathcal{L}, (\text{op}, i, B))$ : Operates in the same manner defined in Definition 2.

## 6.2. Security proof

We now prove that Construct 1 satisfies the correctness and security requirements of Section 4.

**Theorem 1 (Correctness)** The tri-op redactable blockchain  $3\mathcal{RBC}_{\text{tv}}$  is **correct** per Definition 3.

**Proof** We prove that both correctness conditions hold.

**Condition (1):** Algorithm  $\text{Create}(pk, \mathcal{L}, C)$  generates a block  $B := (C, (\text{MaxV}(\vec{V}), \text{apd}, \ell + 1), \epsilon)$ . The block content of  $B$  is  $C$ . Furthermore, the version of  $B$  is correctly computed as required by  $\Phi$ : The version triplet includes a globally unique version number, the operation is valid, and the index is in  $\text{Ind}_\ell(\text{apd})$ . Finally, if  $\mathcal{L}$  is already a valid chain, so is  $\mathcal{L}^* := \mathcal{L} + [B]$ . This is because  $\psi$  returns 1 on all blocks in  $\mathcal{L}^*$  prior to the last block (due to the validity of  $\mathcal{L}$ ). For the last block  $B$ , since  $\text{Version}_{\text{op}}(B) = \text{apd}$ , the return value of  $\psi(pk, B)$  is trivially 1. As a result, all blocks verify, and  $\Psi$  returns 1 as well.

**Condition (2):** Algorithm  $\text{Redact}(sk, \mathcal{L}, (\text{op}, i, C))$  generates  $\perp$  if  $\text{op} \notin \{\text{chg}, \text{rem}, \text{ins}\}$  or  $\text{op} \notin \text{Ind}_\ell(\text{op})$ . Otherwise, it returns  $B := (C, (\text{MaxV}(\vec{V}), \text{op}, i), W)$ . The block content of  $B$  is  $C$ . Furthermore, the version of  $B$  is correctly computed as required by  $\Phi$ : The version triplet includes a globally unique version number, the operation is a valid redaction, and index is in  $\text{Ind}_\ell(\text{apd})$ . Finally, if  $\mathcal{L}$  is already a valid chain, so is  $\mathcal{L}^* := \text{Transform}(\mathcal{L}, (\text{op}, i, B))$ . This is because  $\psi$  returns 1 on all blocks in  $\mathcal{L}^*$  prior to the last block (due to the validity of  $\mathcal{L}$ ). For the last block  $B$ , due to Equation (18),  $W$  is a valid signature on  $C \parallel V$ . Hence, the return value of  $\psi(pk, B)$  is 1, as per Equation (17). □

**Theorem 2 (Security)**  $3\mathcal{RBC}_v$  is *secure* per Definition 4, assuming  $(\text{GenSig}, \text{Sign}, \text{VerifySig})$  is an *sUF-CMA* signature scheme as defined in Definition 1.

**Proof** For any (efficient) adversary  $\mathcal{A}$ , who wins in Section 4 with probability  $\epsilon$ , we construct an efficient forger  $\mathcal{F}$ , who forges a signature with the same probability.

The forger  $\mathcal{F}$  is given as input the public key  $pk$  of the signature scheme, and can query the signing oracle  $\text{Sign}_{sk}(\cdot)$  polynomially many times. It initializes the set  $\text{Hist}$  to empty, and the ledger  $\mathcal{L}$  as specified by Construct 1. It then executes the adversary  $\mathcal{A}(pk, \mathcal{L})$  as a subroutine. Whenever the adversary makes an oracle request, the forger responds as specified next:

- **Queries to the redaction oracle**  $\text{REDC}(\text{op}, i, C)$ : If either  $\text{op} \notin \{\text{chg}, \text{ins}, \text{rem}\}$  or  $i \notin \text{Ind}_\ell(\text{op})$ , the forger  $\mathcal{F}$  returns 0 and halts. Otherwise,  $\mathcal{F}$  creates a new block  $B := (C, V, W)$  with content  $C$ , version triplet  $V := (\text{MaxV}(\vec{V}), \text{op}, i)$  and witness  $W$ . To compute the witness,  $\mathcal{F}$  sends the query  $(C \parallel V)$  to the signing oracle. It then sets  $\text{Hist} := \text{Hist} \cup \{(\text{op}, i, B)\}$ , and finally returns  $B$  to the adversary  $\mathcal{A}$  for further processing.
- **Queries to the installation oracle**  $\text{INST}(\text{op}, i, B)$ : The forger  $\mathcal{F}$  acts exactly as in Step 4 of Section 4. That is, it calls the underlying  $\text{Install}$  operation, and returns 0 and halts if the installation fails. If the installation succeeds on an append or a nonfresh redaction,  $\text{Hist}$  is cleared and the game continues. Otherwise, the adversary is successful in the game. In this case, the forger  $\mathcal{F}$  parses  $B$  as the triple  $(C, V, W)$ . Since the installation algorithm returns 1, we know that  $B$  is a valid block. In particular,  $W$  is a valid signature on the message  $m \stackrel{\text{def}}{=} (C \parallel V)$ . In this case,  $\mathcal{F}$  returns  $(m, W)$  as a valid forgery.

It remains to show that the returned pair is fresh, meaning that the signing oracle has never returned the signature  $W$  when queried on input  $m$ . The forger has already checked that  $(\text{op}, i, B)$  is not in the set  $\text{Hist}$  (as in Step 4 of Section 4). Therefore, we consider all the remaining cases:

1.  **$B$  was returned at some point by the REDC oracle but was removed from Hist by a subsequent call to INST:** This is impossible because once  $\text{INST}$  is called, the maximum version in the ledger is increased. Therefore, no previously obtained  $B$  remains valid.

2.  $(\text{op}', i', B) \in \text{Hist}$ , **where**  $(\text{op}', i') \neq (\text{op}, i)$ : This is impossible, as  $B$  includes as part of its version both the operation and the location. Changing any of those causes  $\Phi$  to return 0.
3.  $(\text{op}, i, B') \in \text{Hist}$  **for some block**  $B' = (C, V, W')$ : In this case, both blocks  $B$  and  $B'$  have the same content and version, but differ in their witnesses. As a result, both  $W$  and  $W'$  verify as signatures on the message  $m \stackrel{\text{def}}{=} (C \parallel V)$ . This constitutes a *strong signature forgery*, and therefore  $(m, W)$  is a valid strong forgery on the underlying signature scheme.
4. **None of the above**: In this case,  $m \stackrel{\text{def}}{=} (C \parallel V)$  is new, and  $W$  is a valid signature on it. This constitutes a *normal signature forgery*, and  $\mathcal{F}$  can output  $(m, W)$  as a valid forgery.

As explained above, cases 1 and 2 are impossible: the adversary never wins the game in these cases, because her output is simply invalid. In plausible cases 3 and 4, the forger generates a valid signature whenever the adversary succeeds. Subsequently,  $\mathcal{F}$  generates a valid signature forgery with the same probability that  $\mathcal{A}$  succeeds in Section 4, and the theorem follows.  $\square$

### 6.3. Experiments

It is noteworthy that redaction operations should occur rather infrequently, as the need for correcting issues in the ledger should rarely occur. That said, it is interesting to show how simple and efficient our construct is. For this reason, we implemented the protocol in the Java programming language. The source code is available on GitHub.<sup>4</sup> It incorporates 18 unit tests that perform the correctness checks (e.g., an administrator can always perform redactions) and security checks (e.g., an invalid or an old redaction cannot be installed). It uses the *Java Microbenchmark Harness (JMH)* framework to measure the throughput of various operations (sign, verify, and redaction with or without installation). We assume the administrator has local access to the ledger and a long queue of operations to be performed. That is, no network delay is incurred. The implementation uses Edwards-curve Digital Signature Algorithm (Ed25519). Section 8.4 of the RFC 8032 explains why the signature is strongly unforgeable. We performed the operations on blocks of size 10,000 bytes, and a ledger with 100,000 blocks. Each benchmark is run for 2 min, for a total of 16 min for all 8 benchmarks. Table 2 shows the benchmark results and the efficiency of our solution.

**Table 2.** The score (average throughput) for various operations, as well as the error, measured in terms of operations per second. The error represents the confidence interval with 99.9% confidence level, assuming a normal distribution. The benchmarks are performed on an Apple 2020 laptop with M1 chip and 16 GB of memory.

| Operation        | Score (ops/s) | Error (ops/s) |
|------------------|---------------|---------------|
| Sign             | 1993.868      | $\pm 62.613$  |
| Verify           | 2154.005      | $\pm 66.021$  |
| Change           | 1984.024      | $\pm 7.232$   |
| Insert           | 1976.893      | $\pm 20.512$  |
| Remove           | 1958.584      | $\pm 68.914$  |
| Change & install | 1031.999      | $\pm 7.846$   |
| Insert & install | 1011.839      | $\pm 4.798$   |
| Remove & install | 1023.124      | $\pm 4.398$   |

<sup>4</sup><https://github.com/msdousti/TriOpRedactableBlockchain>



## 7. Summary and future work

In this paper, we defined a model for redactable blockchains that, for the first time, incorporated all three types of redactions: block change, block removal, and block insertion. We showed that enabling block insertions renders previous constructs susceptible to either “twin-block attack” or “change-of-operation attack”. We then proposed a new construct that is proved secure in this tri-op model.

While our model is simple enough to capture many types of attacks, it is still an abstraction of the real world. In particular, it does not capture the distributed nature of blockchains: the model is designed as a game between an adversary and a challenger. It is a first step toward understanding the diversity of attacks and proofreading existing constructs. However, a distributed model would better capture all types of real-world attacks, such as the case where a new party joins the network and receives contradicting versions of the ledger from existing parties. For further discussions on the choice of model, the reader is referred to [8]. Therefore, the next logical step is to cast our model in a multiparty setting similar to [15]. Only then can one be sure that the constructs proven secure can in fact be used in the real-world setting.

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