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## Design of a sharp response microstrip lowpass filter using taper loaded and radial stub resonators

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**Abstract:** This paper proposes a compact microstrip lowpass filter with a wide stopband and a very sharp roll-off. This structure consists of two dual taper-loaded resonators that are connected to the radial stubs. The resonators are described using an LC model, and its Z- and S-parameters are extracted as a function of the LC component. In the proposed filter, cut-off frequency is placed at 1.76 GHz, roll-off rate is higher than 142 dB/GHz, insertion loss is less than 0.42 dB from DC to 1.5 GHz, and rejection is greater than –24 dB from 1.88 to 15.2 GHz. The proposed filter is designed, fabricated, and measured, and the measured values are in good agreement with the EM-simulated results.

**Key words:** Lowpass filter, circuit model, scaling, EM simulation

### 1. Introduction

Microstrip lowpass filters (LPFs) with compact size and high performance are widely applied in communication systems for suppression of unwanted signals. These filters appear in various shapes. Nevertheless, in the designing process of the novel structures, the main purpose is to improve the response parameters such as stopband bandwidth, selectivity, and compactness. Researchers have used different methods to realize these goals. Several articles have focused on sharpness improvement [1–3]. In [1], a compact LPF with high selectivity is obtained by combining three shunt open stubs. A compact structure with high selectivity was designed in [2], which is composed of two folded stepped impedance open stubs. In [4–8], researchers designed LPFs with a wide stopband. In [4], a novel meandered-slot resonator was presented to design an LPF with a wide stopband. This LPF reaches an ultrawide stopband of 12.8 times the cut-off frequency and with attenuation higher than 20 dB. A bandstop structure has been embedded into a classical stepped impedance LPF in [7] to increase the width of the stopband. This filter has a small size. A high-performance LPF with a compact size, wide stopband, and sharp rejection has been proposed in [9]. In [10], a symmetrical coupled line has been proposed to design a wide stopband LPF. The authors in [11–14] focus on compactness in LPF design.

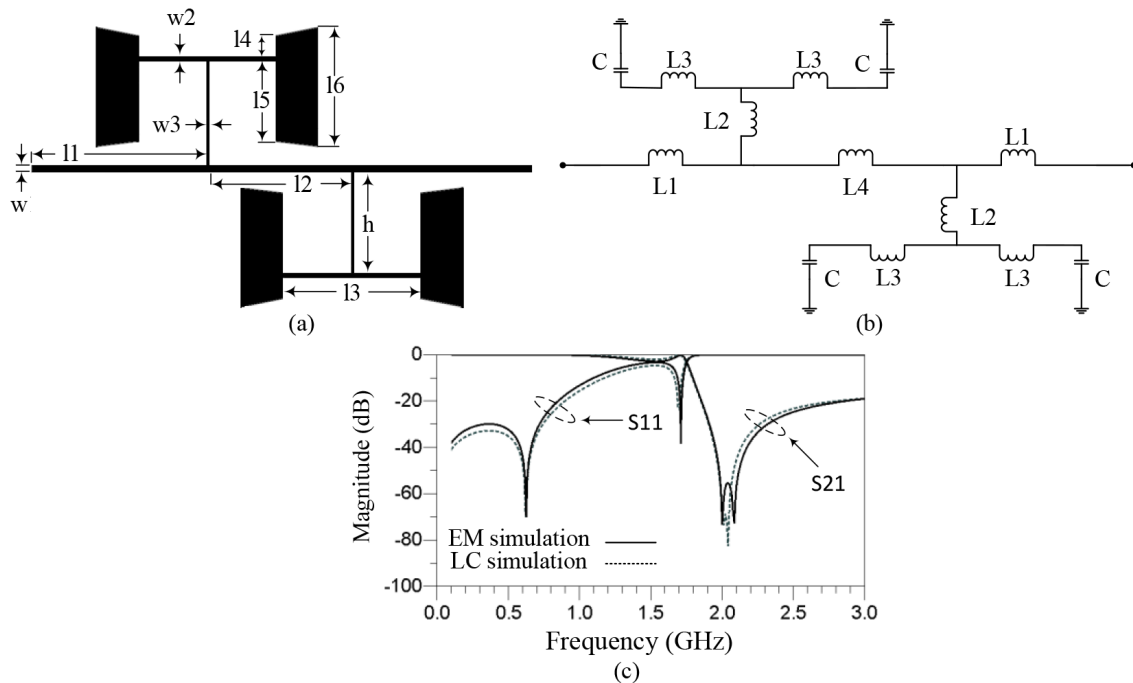
In this paper, we propose a new structure for the design of an LPF with very sharp rejection, wide stopband, and compact size. Initially, the proposed dual taper-loaded resonator is presented and studied, and then it is used to implement a high-performance LPF. The resonators are described using the LC model, and their Z- and S-parameters are extracted as a function of the LC component. In the proposed filter, the cut-off frequency is placed at 1.76 GHz, the roll-off rate is higher than 142 dB/GHz, and the circuit size is  $0.215 \lambda_g \times$

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$0.1 \lambda_g$ . This LPF achieves a wide stopband with an overall 24-dB attenuation up to 7.56 times the 3-dB cut-off frequency.

## 2. Proposed structure

The layout of the proposed structure is shown in Figure 1a. In this resonator, two taper-loaded cells are connected with a central simultaneity point. This resonator creates two near-band attenuation zeros that result in a sharp roll-off and a deep rejection in the low-frequency region of the stopband. The dimensions in Figure 1a are:  $l_1 = 7.75$  mm,  $l_2 = 6.3$  mm,  $l_3 = 6.1$  mm,  $l_4 = 0.95$  mm,  $l_5 = 3.55$  mm,  $l_6 = 5.2$  mm,  $w_1 = 0.2$  mm,  $w_2 = 0.2$  mm,  $w_3 = 0.1$  mm,  $w_4 = 1.83$  mm, and  $h = 4.6$  mm. This resonator is designed on an RT/Duroid 5880 substrate with 2.2 dielectric constant, 15 mil height, and 0.0009 loss tangent. Figure 1b shows the approximate equivalent LC circuit of the proposed resonator. The parts of this circuit are introduced and then the behavior of the resonator is studied.



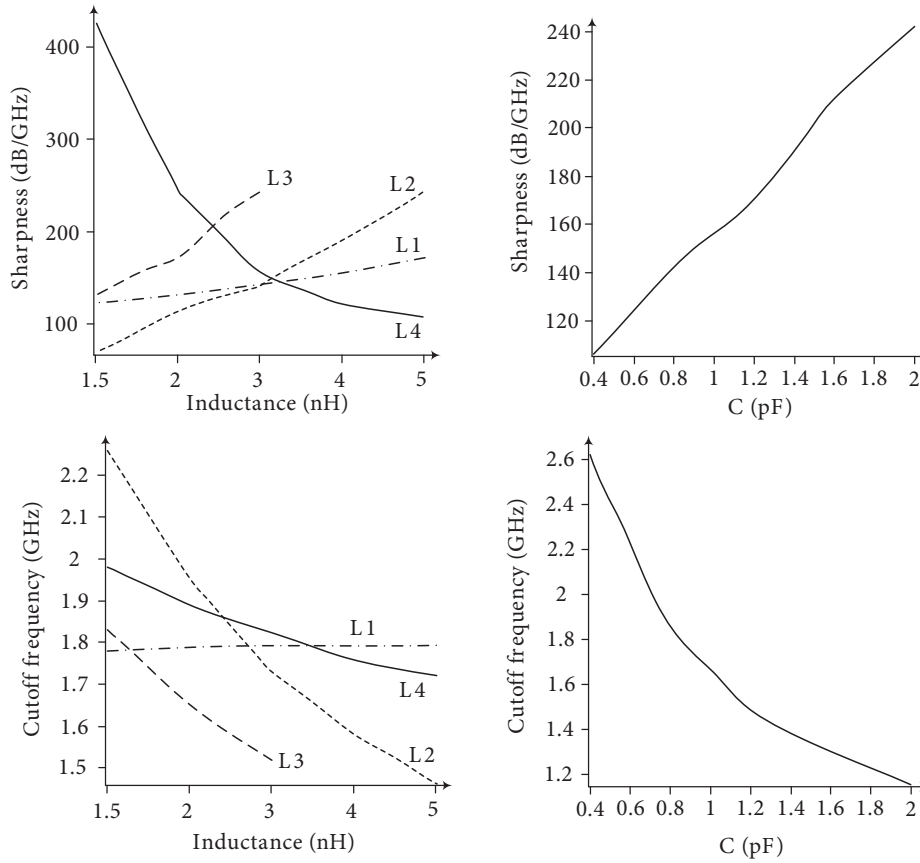
**Figure 1.** Proposed resonator: a) layout, b) equivalent LC circuit, c) EM and LC simulation.

$L_1$  and  $L_4$  are inductances of the central transmission line. The inductances of the T-shaped line are introduced by  $L_2$  and  $L_3$ .  $C$  shows the body capacitance of the tapered shape.

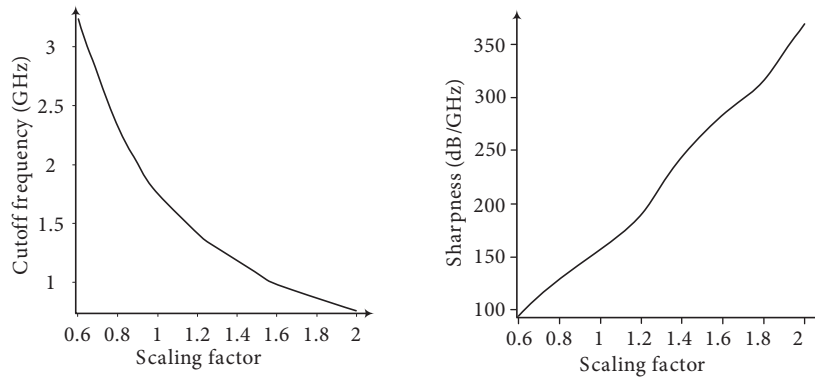
The calculated characteristic impedance ( $Z_c$ ) and effective permittivity ( $\epsilon_{re}$ ) are  $Z_c = 154 \Omega$  and  $\epsilon_{re} = 1.695$  for  $w = 0.1$ ,  $Z_c = 123 \Omega$  and  $\epsilon_{re} = 1.728$  for  $w = 0.2$ , and  $\epsilon_{re} = 1.94$  and  $Z_c = 36.5 \Omega$  for  $w = 1.83$ . The LC parameters are calculated as follows [2], [15–16]:  $L_1 = 3.2$  nH,  $L_2 = 2.7$  nH,  $L_3 = 1.4$  nH,  $L_4 = 3.52$  nH, and  $C = 0.84$  pF.

The LC and EM simulated results of the resonator are shown in Figure 1c.

Figures 2 and 3 show two synthesis methods to adapt the proposed resonator to different specifications. The sharpness and the cut-off frequency of the LC resonator as a function of  $L_1, L_2, L_3, L_4$ , and  $C$  are shown in Figure 2.



**Figure 2.** Sharpness and cut-off frequency of the LC resonator as a function of L1, L2, L3, L4, and C.



**Figure 3.** Sharpness and cut-off frequency of the resonator as a function of the scaling factor.

Another synthesis method is presented using resonator scaling. Figure 3 shows the sharpness and cut-off frequency of the resonator as a function of the scaling factor (scaling all the resonator dimensions with a constant factor).

The  $Z_{21} = Z_{12}$  and  $Z_{11} = Z_{22}$  of the proposed LC resonator are a function of L2, L3, L4, C, and f, as follows:

$$\begin{aligned}
|Z_{21}| = |Z_{12}| = & 0.125I(8\pi^2 f^2 CL2 + \\
& 4L3\pi^2 f^2 C - 1)^2 / C\pi f(8L2\pi^2 f^2 C + \\
& 4\pi^2 f^2 CL3 + 4\pi^2 f^2 CLA - 1)
\end{aligned} \tag{1}$$

$$\begin{aligned}
|Z_{11}| = |Z_{22}| = & 0.125I(1 + 64\pi^4 f^4 C^2 L2L4 + \\
& 32\pi^4 f^4 C^2 L3L4 - 8L4\pi^2 f^2 C + 64\pi^4 f^4 C^2 L2^2 + \\
& 64\pi^4 f^4 C^2 L2L3 - 16\pi^2 f^2 CL2 + 16\pi^4 f^4 C^2 L3^2 - \\
& 8\pi^2 f^2 CL3 + 128\pi^4 f^4 C^2 L2L1 + 64\pi^4 f^4 C^2 L1L3 - \\
& 16\pi^2 f^2 CL1 + 64\pi^4 f^4 C^2 L1L4) / \\
& c\pi f(8L2\pi^2 f^2 C + 4\pi^2 f^2 CL3 + 4\pi^2 f^2 CLA - 1)
\end{aligned} \tag{2}$$

$|S_{21}|$  of the LC resonator is as follows:

$$\begin{aligned}
|S_{21}| = & (12.5I(8\pi^2 f^2 CL2 + 4\pi^2 f^2 CL3 - 1)^2) / \\
& (c\pi f(-1 + 8L2\pi^2 f^2 C + 4\pi^2 f^2 CL3 + 4\pi^2 f^2 CLA) \\
& (((0.125I(-1 + 8L2\pi^2 f^2 C + 4\pi^2 f^2 CL3) \\
& (-1 + 8L4\pi^2 f^2 C + 8\pi^2 f^2 CL2 + 4\pi^2 f^2 CL3) / \\
& (c\pi f(-1 + 8L2\pi^2 f^2 C + 4\pi^2 f^2 CL3 + 4\pi^2 f^2 CLA) \\
& + 50)^2 + 0.0156(-1 + 8L2\pi^2 f^2 C + 4\pi^2 f^2 CL3)^4 / \\
& (c^2 \pi^2 f^2 (-1 + 8L2\pi^2 f^2 C + 4\pi^2 f^2 CL3 + 4\pi^2 f^2 CLA)^2)))
\end{aligned} \tag{3}$$

where  $f$  represents the frequency at Hz. If in Eq. (3) we set  $L1 = 3.2$  nH,  $L2 = 2.7$  nH,  $L3 = 1.4$  nH,  $L4 = 3.52$  nH, and  $C = 0.84$  pF, then  $|S_{21}|$  turns to a function of  $f$  as in Eq. (4):

$$\begin{aligned}
|S_{21}| = & (1.48810^{13} I(-1 + 2.28510^{-20} \pi^2 f^2)^2) / \\
& (\pi f(-1 + 3.4710^{-20} \pi^2 f^2))((1 / \\
& (\pi f(-1 + 3.4710^{-20} \pi^2 f^2))(1.48810^{11} I \\
& (-1 + 2.28510^{-20} \pi^2 f^2)(-1 + 4.6510^{-20} \pi^2 f^2)) + \\
& 50)^2 + (2.2110^{22} (-1 + 2.28510^{-20} \pi^2 f^2)^4) / \\
& (\pi^2 f^2 (-1 + 3.4710^{-20} \pi^2 f^2)))
\end{aligned} \tag{4}$$

To verify the validity of these equations, Figure 4 shows the magnitude of  $S_{21}$  as a function of  $f$  (according to Eq. (4)).

The sharpness of the resonator is introduced by Eq. (5):

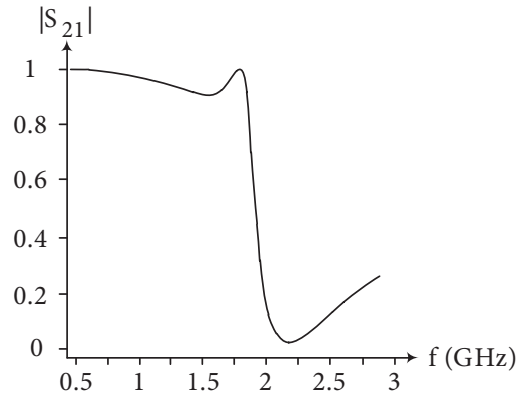
$$\Delta f = f_s - f_c, \tag{5}$$

where  $f_s$  is the first  $-20$  dB point and  $f_c$  is the 3dB cut-off frequency of the resonator. Let  $f_c$  be the smallest positive root of Eq. (6) and  $f_s$  denote the positive root of Eq. (7). Then Eq. (5) defines the sharpness of the LC resonator response.

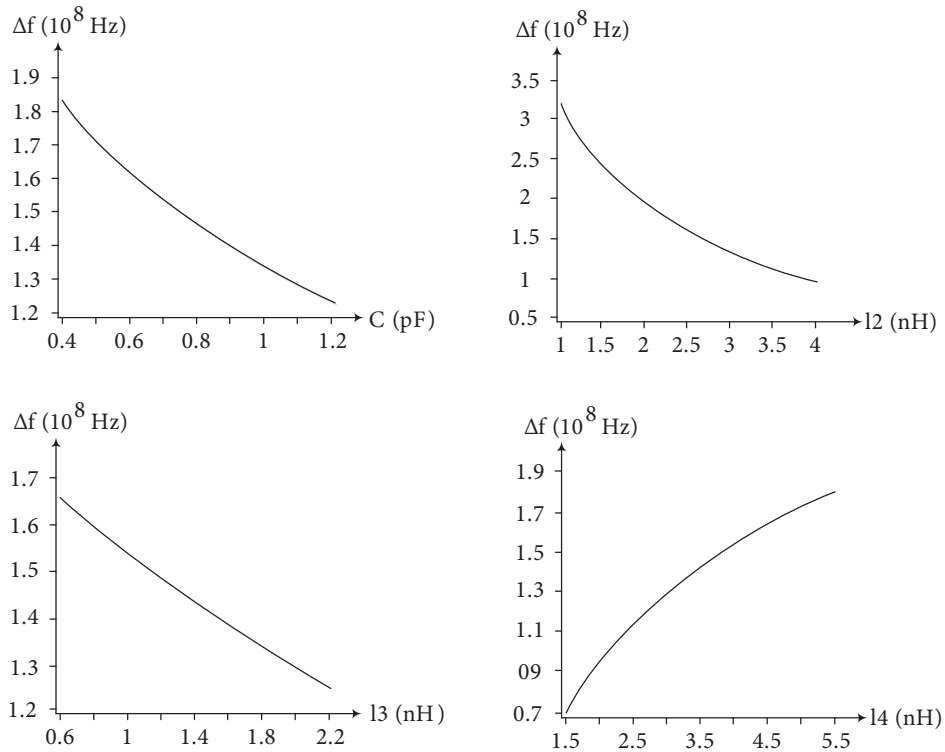
$$A = 20 \log |S_{21}(f)| + 3 = 0 \tag{6}$$

$$B = 20 \log |S_{21}(f)| + 20 = 0 \tag{7}$$

Figure 5 depicts  $\Delta f$  in terms of  $C$ ,  $L2$ ,  $L3$ , and  $L4$ .



**Figure 4.** Magnitude of the  $S_{21}$  as a function of  $f$ , according to Eq. (4).

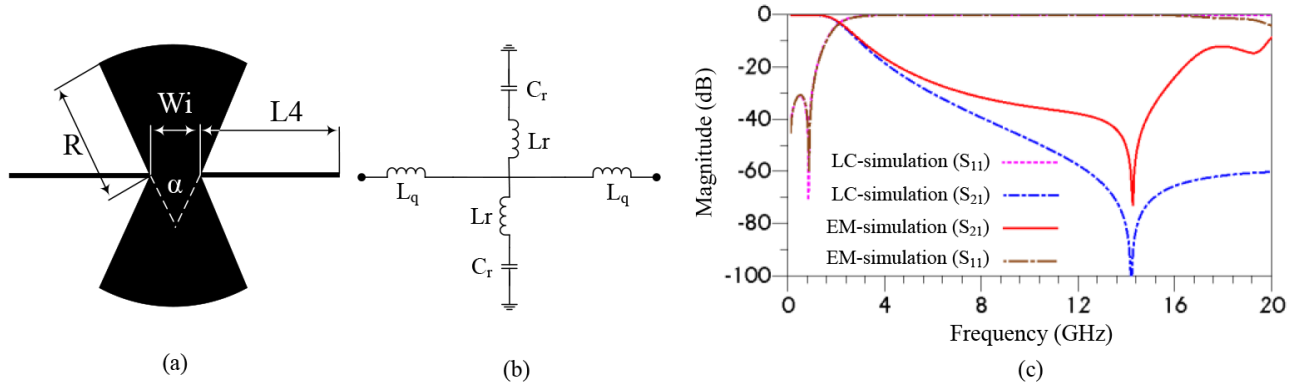


**Figure 5.** Sharpness of the LC resonator response as a function of  $C$ ,  $L_2$ ,  $L_3$ , and  $L_4$ .

### 3. Filter design and results and discussion

Figure 1c shows the simulated response of the proposed resonator, which has a limited stopband and low rejection. To solve this problem, two patched radial stubs are cascaded with the resonator to form the proposed filter. Figure 6 shows the layout, equivalent LC model, and LC/EM simulation results of the radial stub resonator. In this model, the series-connected  $L_r$  and grounded  $C_r$  introduce the radial stub, and  $L_q$  represents the inductance of the central line. The dimensions of this structure are as follows:  $w_i = 2$  mm,  $l_4 = 6.2$  mm,  $r = 4.7$  mm, and  $\alpha = 54^\circ$ .

Using Eqs. (8–11) and some optimization [2,15–16], these LC parameters are calculated as  $L_r = 0.09$



**Figure 6.** Radial stub resonator: a) layout, b) equivalent LC model, c) LC/EM simulation results.

nH,  $C_r = 1.4$  pF, and  $L_q = 4.2$  nH.

$$L = \frac{lz_c}{v_p} \quad (8)$$

$$v_p = \frac{c}{\sqrt{\epsilon_{re}}} \quad (9)$$

For  $w/h \leq 1$

$$\epsilon_{re} = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \left\{ \left[ 1 + 12 \frac{h}{w} \right]^{-0.5} + 0.04 \left[ 1 - \frac{w}{h} \right]^2 \right\}, \quad z_c = \frac{\eta}{2\pi\sqrt{\epsilon_{re}}} \ln \left[ 8 \frac{h}{w} + 0.25 \frac{w}{h} \right] \quad (10)$$

For  $w/h \geq 1$

$$\epsilon_{re} = \frac{\epsilon_r + 1}{2} + \frac{\epsilon_r - 1}{2} \left[ 1 + 12 \frac{h}{w} \right]^{-0.5}, \quad z_c = \frac{\eta}{\sqrt{\epsilon_{re}}} \left\{ \frac{w}{h} + 1.393 + 0.677 \ln \left[ \frac{w}{h} + 1.444 \right] \right\}^{-1} \quad (11)$$

Figure 7 shows the sharpness and cut-off frequency of the LC radial stub resonator as a function of  $L_r$ ,  $C_r$ , and  $L_q$ .

Sharpness and cut-off frequency of the radial stub resonator as a function of the scaling factor are shown in Figure 8.

$\Delta f_1$  has been calculated using the  $S_{21}$  function of the radial stub resonator, similarly to the  $\Delta f$  for the LC radial stub resonator. Figure 9 shows the  $\Delta f_1$  as a function of  $L_r$ ,  $C_r$ , and  $L_q$ .

Figure 10 shows the layout, photograph, and simulation results of the proposed filter. The dimensions of the proposed filter are as follows:

$w_1 = 1.15$  mm,  $w_i = 2$  mm,  $m_1 = 2.5$  mm,  $m_2 = 3$  mm,  $m_3 = 7.7$  mm,  $m_4 = 6.2$  mm,  $h_1 = 4.6$  mm,  $h_2 = 4.87$  mm,  $h_3 = 4.55$  mm,  $h_4 = 4.6$  mm,  $r = 4.7$  mm, and  $\alpha = 54^\circ$ .

The simulation was accomplished using an EM simulator (ADS), and measurements were performed using an Agilent network analyzer N5230A. As depicted in Figure 10c, the 3-dB cut-off frequency is placed at 1.76 GHz, and a stopband is reached from 1.88 to 15.2 GHz with a higher than 24 dB attenuation level. The insertion loss is less than 0.4 dB from DC to 1.5 GHz. The return loss is higher than 11 dB in the passband and is close to 0 dB in the stopband.

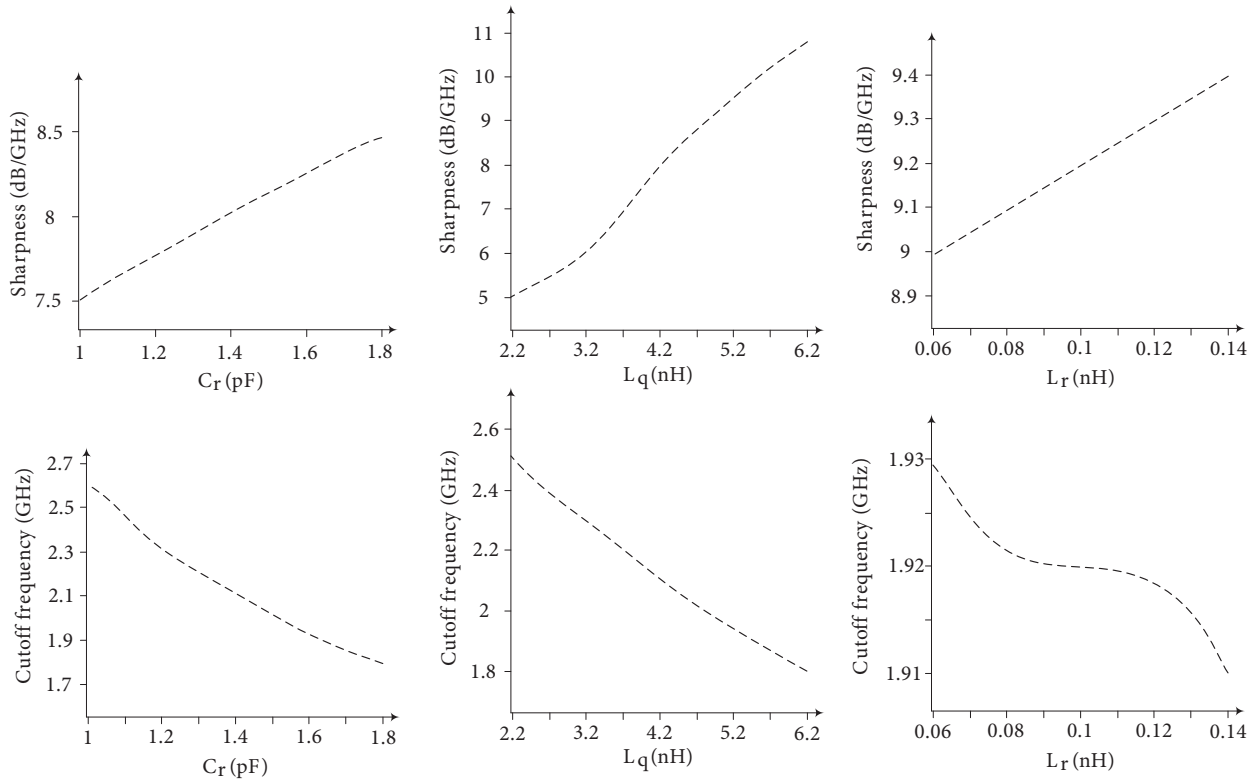


Figure 7. Sharpness and cut-off frequency of the LC radial stub resonator as a function of  $L_r$ ,  $C_r$ , and  $L_q$ .

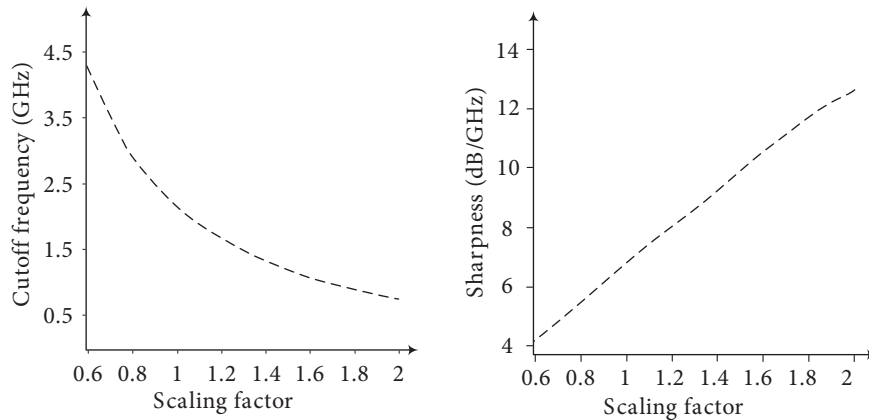


Figure 8. Sharpness and cut-off frequency of the radial stub resonator as a function of the scaling factor.

Table 1 compares the performance of the proposed filters in terms of stopband bandwidth, rejection level in the stopband, sharpness, physical size, and passband losses level with the previous works. This comparison is based on the equations and parameters of Table 2 [9,13]:

$\alpha_{max}$ ,  $\alpha_{min}$ ,  $f_s$ ,  $f_c$  and  $\lambda_g$  are introduced in Table 3.

As shown in Table 1, the response of the proposed filter is sharper than in [1,2,4,5,7-14], its stopband bandwidth is wider than in [1-3,5,7,8,10-14], its rejection level is better than in [1,2,4-8,10-14], and normalized circuit size of the proposed filter is better than in [1,2,4-7,10,11,14].



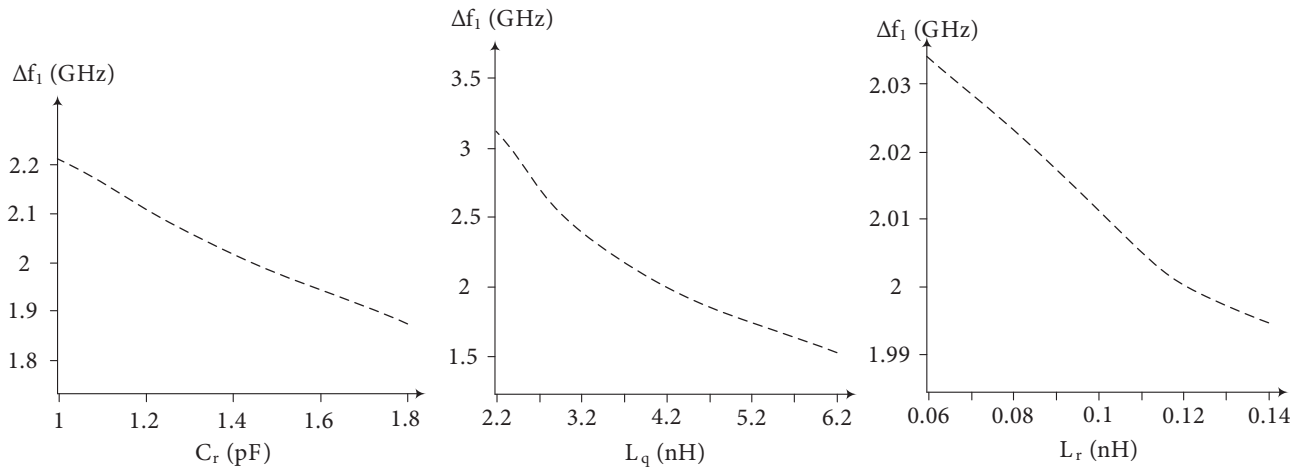


Figure 9.  $\Delta f_1$  as a function of  $L_r$ ,  $C_r$ , and  $L_q$ .

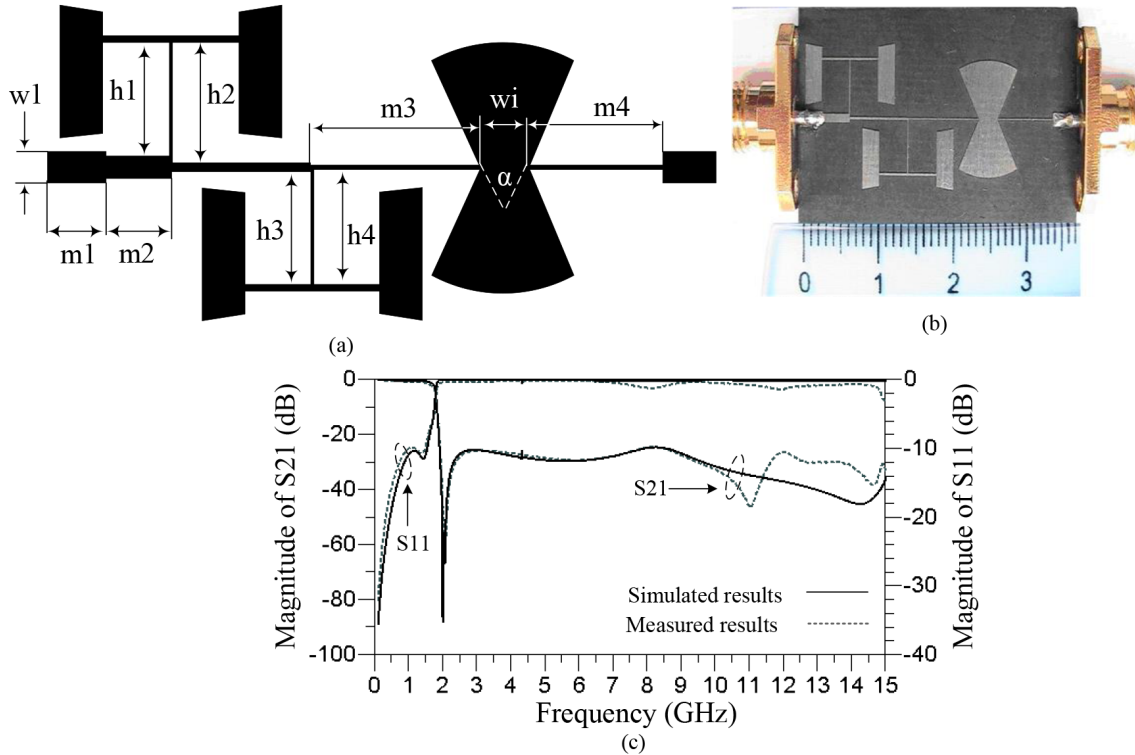


Figure 10. Proposed filter: a) layout, b) photograph, c) simulation and measurement results.

#### 4. Conclusion

In this paper, a high-performance lowpass filter, based on taper loaded units, is designed, fabricated, and measured. The physical size of the filter is  $0.215 \lambda_g \times 0.1 \lambda_g$ . The measured results indicate a wide stop-band of 13.32 GHz with an attenuation level higher than 24 dB and a very sharp transition band with a rate of 142 dB/GHz. Its compactness, sharp rejection, and wide stopband make this LPF suitable for microwave applications.

**Table 1.** Performance comparison among proposed filter and referenced works.

Article	fc (GHz)	SBW (GHz)	MA (dB)	$\zeta$ (dB/GHz)	NCS	IL (dB)	RL (dB)
This work	1.76	13.32	24	142	0.0215	0.4	11
[1]	2.49	4.2	20	54.8	0.0323	0.26	22
[2]	2.28	12.47	20	121.4	0.0338	0.14	12.3
[3]	1.49	5.76	20	134.55	0.1495	0.85	13.5
[4]	2.2	28.16	20	58.6	0.055	0.5	10
[5]	1.76	12.32	20	51.5	0.048	0.6	8.5
[6]	1.8	29.7	20	250	0.251	0.3	-
[7]	1.8	5.04	16	34	0.031	0.5	10
[8]	2	10.3	20	24.29	0.0094	0.6	12
[9]	1.89	17.94	25	121.5	0.0177	0.5	10
[10]	0.8	6.42	16	68	-	0.1	27
[11]	2.2	5.28	23	85	0.051	< 0.5	13
[12]	1.3	12.22	17	21	0.0088	0.3	-
[13]	1.18	7	15	36.3	0.0062	-	> 20
[14]	3.09	15.17	20	45.95	0.031	0.5	10

**Table 2.** Basic parameters for comparing LPF responses.

Parameters	Symbol	Equation or definition
Stopband bandwidth (GHz)	SBW	Stopband bandwidth of the LPF response
Rejection level in stopband (dB)	MA	Max attenuation level in the stopband
Sharpness (dB/GHz)	$\zeta$	$\zeta = \frac{\alpha_{max} - \alpha_{min}}{f_s - f_c}$
Normalized circuit size	NCS	$NCS = \frac{\text{physical size}}{\lambda_g^2}$
Passband losses level (dB)	IL	Passband ripple level
	RL	Return loss in passband

**Table 3.** Description of the  $\alpha_{max}$ ,  $\alpha_{min}$ ,  $f_s$ ,  $f_c$ , and  $\lambda_g$ .

Phrase	Description
$\alpha_{max}$	3 dB attenuation point
$\alpha_{min}$	20 dB attenuation point
$f_s$	20 dB stopband frequency
$f_c$	3 dB cut-off frequency
$\lambda_g$	Guided wavelength at 3 dB cut-off frequency

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