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The Lattice Dynamics of γ -Iron

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Abstract

Lattice dynamical calculations are performed on γ -iron using the Clark-Gazis-Wallis (CGW) model to represent the ion-ion interactions, and a modified form of the Sharma-Joshi model to include ion-electron interactions. The theory is used to compute the phonon dispersion curves, frequency spectra and the lattice specific heat of γ -iron. The obtained results are in good agreement with the experimental findings, and are better than those calculated using the other theories.

Introduction

As is well known, iron is bcc α -phase at low temperature and it undergoes transformation to the fcc γ -phase at approximately 1200K, then transforms to bcc δ -phase at approximately 1670K. Because of its technological importance, many papers exist in the literature on the lattice dynamics of bcc iron [1-4], but fewer investigations are published for γ -iron [5,6,7], the reason being the difficulty of growing *in situ* single crystals for γ -iron. After Zarestky and Stassis measurement [8] of γ -iron phonon frequencies at high temperature the present work is the fourth theoretical study on the lattice dynamics of γ -iron.

Okoye and Pal [7] computed the phonon frequencies of γ -Fe within the frame work of the transition metal model potential (TMMP) approach of Animalu [9], including the contribution of the short-range three-body interactions. Since the d-electrons and the conduction electrons present in the transition metals significantly affect the lattice dynamical behavior in γ -iron, the TMMP approach does not give very good agreement with experiments (mainly for the trasverse modes of vibration) and thus is limited as a model. Moreover, transition metals pseudopotential and second-order pertubation theories are also inadequate and unsatisfactory for γ -iron [7].

Singh and Rathore [6], approached the problem using a pairwise potential giving higher frequencies than those of experiment, mainly in the longitudinal branches. Al-

though the pairwise potential produces the same dynamical matrix as those of the DAF (de Launay Angular Force) model [10,11,12], its dynamical matrix is not rotationlaly invariant [11].

In this paper, we have used the CGW angular force model, developed orginally by Clark-Gazis-Wallis [2], and have included ion-electron interactions following the scheme of Behari and Tripathi [13,14,15]. The CGW model guarantes rotational invariance for the resulting dynamical matrix [11,16,17], and gives a dynamical matrix different from the DAF model for fcc metals [18].

Theory and Computation

Secular Determinant

The phonon frequencies in the harmonic approximation are given by the usual secular equation

$$|D_{\alpha\beta}(\vec{k}) - m\omega^2 I\delta_{\alpha\beta}| = 0, \quad (1)$$

where

$$D_{\alpha\beta}(\vec{k}) = D_{\alpha\beta}^{i-i}(\vec{k}) + D_{\alpha\beta}^{i-e}(\vec{k}). \quad (2)$$

Here, $D_{\alpha\beta}(\vec{k})$ are the elements of the dynamical matrix, (\vec{k}) is the wave vector confined to the first Brillouin zone, I is the unit matrix of order three and m is the ionic mass. In this present scheme the ion-ion interaction $D_{\alpha\beta}^{i-i}(\vec{k})$ is represented by the CGW model, which is effective up to second neighbours, and the ion-electron interaction $D_{\alpha\beta}^{i-e}(\vec{k})$ is assumed to have the form of the Behari and Tripathi model [15].

The elements of the dynamical matrix in Eq.(1) for fcc structure are given by Bose *et al.* [18]:

$$\begin{aligned} D_{xx} = & 2 \left[\alpha + \frac{8}{a^2}(\gamma_1 + \gamma_2) \right] [2 - C_1(C_2 + C_3)] + 4\beta S_1^2 \\ & - \frac{4\gamma_1}{a^2} (2 \cos 2\pi a k_1 - \cos 2\pi a k_2 - \cos 2\pi a k_3) \\ & + a^3 \pi^2 k_1^2 k_e G^2(x) \end{aligned} \quad (3)$$

$$D_{xy} = 2 \left(2\alpha - \frac{16\gamma_1}{a^2} \right) S_1 S_2 + a^3 \pi^2 k_1 k_2 k_e G^2(x), \quad (4)$$

where $C_i = \cos \pi a k_i$, $S_i = \sin \pi a k_i$, $G(x) = 3\left(\frac{\sin x - x \cos x}{x^3}\right)$ and $x = 2\pi k \gamma_0 \cdot \alpha, \beta$ and γ_1, γ_2 are the central and angular force constants corresponding to the first and second neighbours, respectively. a, k_i, γ_0 and k_e are the lattice constant, the phonon wave vector compenents, the radius of the Wigner-Seitz sphere and the bulk modulus of the electron

gas, respectively.

Force Constants

By expanding the secular determinant in the long-wavelength limit ($k \rightarrow 0$), one gets the following relations between the elastic constants and the force constants, as in [18]:

$$\begin{aligned}
 aC_{11} &= 2\alpha + 2\beta + \frac{32\gamma_1}{a^2} + \frac{16\gamma_2}{a^2} + ak_e \\
 aC_{12} &= \alpha - \frac{16\gamma_1}{a^2} - \frac{8\gamma_2}{a^2} + ak_e \\
 aC_{44} &= \alpha + \frac{8\gamma_2}{a^2} \\
 m\omega_L^2 &= 8\alpha + \frac{64\gamma_1}{a^2} + \frac{64\gamma_2}{a^2} + ak_e\pi^2 G^2(x) \\
 m\omega_T^2 &= 4\alpha + \frac{32\gamma_1}{a^2} + \frac{32\gamma_2}{a^2},
 \end{aligned} \tag{5}$$

where C_{11}, C_{12} and C_{44} are measured elastic constants; and $\nu_L (= \omega_L/2\pi)$ and $\nu_T (= \omega_T/2\pi)$ are the zone boundary frequencies in [100] direction.

Solutions to Eq (5) give the unknown constants, which are substituted in the dynamical matrix to find the phonon frequencies in the main symmetry directions [100], [110] and [111]. For the present work, the required experimental constants and the calculated parameters are given in Table 1 and Table 2, respectively.

Table 1. Input data [8,19] for computation of force constants.

C_{11}	C_{12}	C_{44}	ν_L	ν_T	a
10^{12}dyn/cm^2	10^{12}dyn/cm^2	10^{12}dyn/cm^2	10^{12}Hz	10^{-10}m	
1.54	1.22	0.77	7.4611	5.3867	3.64

Table 2. The calculated force constants for γ -iron in units of dyn/cm^2 .

γ_1/a^2	γ_2/a^2	α	β	ak_e
-175.192	-936.955	35523.650	1755.136	-1414.378

The obtained force constants are then used to calculate the frequency distribution function, $g(\nu)$, as a function of frequency with the algorithm of Gilat and Raubenheimer [20] and is shown in Fig. 1. It shows very similar trends to that of Zarestky and Stassis's [8] calculations based on the experimental findings. Further, we have also computed the specific heat C_v at different temperatures from the formula [21]

$$C_v = \frac{3R}{3000} \sum_v E(h\nu/kT)g(\nu), \tag{6}$$

where $g(\nu)$ is the frequency distribution function for γ -iron, R the gas constant, and $E(h\nu/kT)$ the Einstein function defined by

$$E(x) = \frac{x^2 e^x}{(e^x - 1)^2}, \quad (7)$$

where $x = h\nu/kT$.

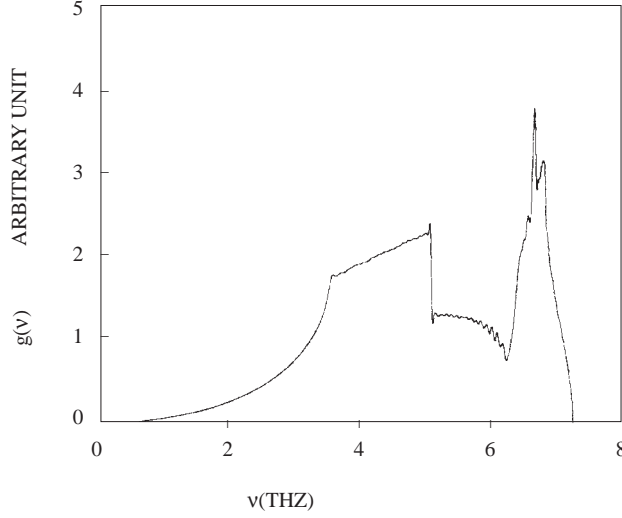


Figure 1. Phonon dispersion curves for γ -iron.

Numerical Results and Discussion

In order to determine the phonon frequencies of γ -iron, we have calculated the ion-ion and ion-electron interaction parts of the dynamical matrix following exactly the procedures in [15,18]. The computed dispersion curves for γ -iron are shown in Fig.2. The experimental values reported by Stassis [8] are also marked in the figure. A close inspection of the figure reveals that the computed curves are in good agreement with the experimental ones in all three symmetry directions except on the zone boundary in the [111] direction. The calculated frequencies in this direction are higher by about of %20 than those measured experimentally. The calculated maximum frequency for γ -iron is about of 7.26×10^{12} Thz, and is in good agreement with that derived from the experimental frequency distributions (7.26×10^{12} Thz). The temperature dependence of specific heat C_v is shown in Fig.3., and it shows the expected behaviour in low ($\theta \leq 10/T$) and high temperature values.

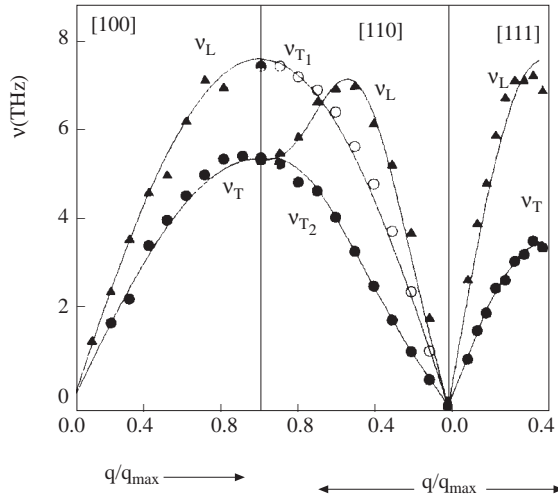


Figure 2. Frequency distribution curve of γ -iron.

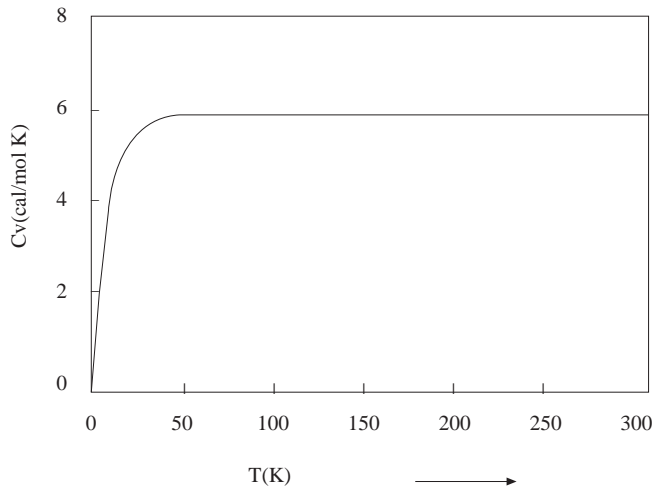


Figure 3. C_v - T curve for γ -iron.

It may be concluded that the present model represents correctly the actual interactions responsible for the lattice vibrations in γ -iron.

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