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On parameter adjustment of the fuzzy neighborhood-based clustering algorithms

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Abstract: Day by day huge amounts data are produced, and evaluation of these data becomes more difficult. The data obtained should provide meaningful, correct, and accurate information. Therefore, all data must be separated into clusters correctly, and the right information from these clusters must be obtained. Having the correct clusters depends on the clustering algorithm that is used. There are many clustering algorithms. The density-based methods are very important among the groups of clustering methods, as they can find arbitrary shapes. An advanced model of the density-based spatial clustering of applications with noise (DBSCAN) algorithm, called fuzzy neighborhood DBSCAN Gaussian means (FN-DBSCAN-GM), is offered in this study. The main contribution of FN-DBSCAN-GM is to find the parameters automatically and to divide the data into clusters robustly. The effectiveness of FN-DBSCAN-GM has been demonstrated on overlapping datasets (six artificial and two real-life datasets). The performances of these datasets are compared with the percentage of correct classification and validity index. Our experiments showed that this new algorithm was a preferable and robust algorithm.

Key words: Cluster analysis, DBSCAN, FN-DBSCAN

1. Introduction

Clustering helps us to collect similar data in the same cluster and separates the different data into different clusters. The density-based spatial clustering of applications with noise (DBSCAN) algorithm is the most well-known algorithm based on densities in the literature [1]. It needs two input parameters (ε and MinPts) for clustering. ε is a distance measure, and Minpts is the minimum number of points. All points in the database are classified into three types: core, border, and noise. If a point is a core point, the number of elements in the ε neighborhood is at least Minpts. In addition, all density-connected points create a cluster in DBSCAN [2].

DBSCAN finds the clusters with different shapes. It is a powerful method because of its positive properties. However, some disadvantages exist in this algorithm [3]. After a small change in input variables, the results show deterioration. In addition, it cannot find clusters with different densities. There are other kinds of density-based clustering algorithms that have been developed to eliminate the disadvantages of the DBSCAN algorithm. DMDBSCAN (dynamic method DBSCAN), LDBSCAN (local-DBSCAN), and EDBSCAN

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(enhanced-DBSCAN) were developed for handling different densities [4–6]. The DBSCAN-GM and VDBSCAN (varied density-based spatial clustering of applications with noise) algorithms were produced for obtaining good clustering without input parameters [7, 8]. Fuzzy neighborhood DBSCAN (FN-DBSCAN) and soft-DBSCAN algorithms were produced for robustness [9, 10]. Fast clustering, active-DBSCAN, and FDBSCAN algorithms were developed [11, 12]. However, the developed algorithms are still inadequate to obtain good clustering [13].

Finding convenient parameters of FN-DBSCAN is a big problem, especially for some datasets [14]. In this study, an algorithm that makes FN-DBSCAN parameter-free is proposed. It is the developed version of study [15]. Note that the above-mentioned VDBSCAN method is also a parameter-free method and it produces clusters with different densities. In addition, it computes k-distances and tries to estimate input parameters of the DBSCAN method. However, the FN-DBSCAN-GM method handled in our study is a fuzzy version of DBSCAN and it tries to estimate input parameters using a statistical test. The rest of this paper is organized into five sections. Clustering algorithms that are necessary for this study are explained in the second section of the paper. The proposed algorithm, called FN-DBSCAN-GM, is described in Section 3. The results from our experiments can be seen in Section 4. The article concludes in Section 5.

2. Background

2.1. K-means algorithm

The K-means algorithm was proposed by MacQueen [16]. The number of clusters, called k, is an input parameter in this algorithm. Data are divided into k clusters by measuring cluster similarity. Each cluster center is calculated by the average value of the coordinates of objects in the cluster. In this algorithm, the first step is to determine the coordinates of k centers. This can be done by various methods. For example, random values or the coordinates of the first k objects can be assigned to the initial center values. After that, Euclid's formula is used for calculating distances between objects and centers as in Eq. (1). x is an object, c is a center, and j is the dimension of these points.

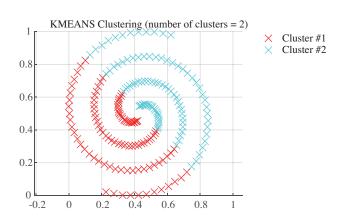
$$d(x,c) = \left(\sum_{i=1}^{j} (c_i - x_i)\right)^{1/2} \tag{1}$$

Each object is assigned to the closest center. New coordinates of centers are recalculated as in Eq. (2). x_h is the point assigned to the cluster. The average of the assigned points determines the new cluster center.

$$newc = \frac{\sum_{h=1}^{n} x_h}{n} \tag{2}$$

These processes are continued as long as there is a difference between the new coordinates of centers and the previous coordinates of those centers. The K-means algorithm has some weaknesses: it needs an input parameter 'k'. Results vary according to the value of k. It is a sensitive algorithm for the noises and initial cluster centers. For example, the results obtained when the first k points are selected as initial cluster centers (Figure 1) are different from the results obtained when random numbers are selected as initial cluster centers (Figure 2). It can be used for numerical data and does not give good results in overlapping sets.

The algorithm of the K-means is as given in Algorithm 1.



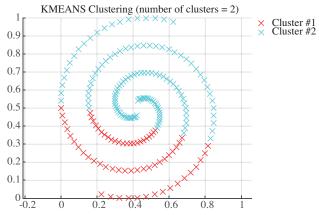


Figure 1. When first two points in the dataset are selected as initial cluster centers.

Figure 2. When two random points are selected as initial cluster centers.

Algorithm 1. K-means algorithm.

- Step 1: k is input. Let k be the number of cluster centers.
- Step 2: Select k cluster centers.
- Step 3: Calculate the distance between each point and cluster centers.
- Step 4: Each point is assigned to the nearest center.
- Step 5: Recalculate the new cluster centers.
- Step 6: If there is a difference between new centers and previous centers, go to Step 3.
- Step 7: End.

2.2. G-means algorithm

The Gaussian means algorithm was developed by Hamerly and Elkan in 2004 [9]. The K-means algorithm has a disadvantage. The optimal value of k must be assigned to provide the best clustering. Automatic estimation of k will be the best solution.

The Gaussian means algorithm makes use of a statistical test to make the decision for the number of clusters. If Gaussian distribution cannot be provided with the number of clusters, the number is increased by 1. The K-means algorithm is run for each increase of it while there is not a Gaussian distribution. k starts from the smallest value, for example 1. It tries to find the correct number of clusters, and so it can find it. The algorithm of Gaussian means (G-means) is as given in Algorithm 2.

Algorithm 2. G-means algorithm.

- Step 1: $S=\{s_i\}$ is the set of the centers.
- Step 2: Use the K-means algorithm for an initial set of centers.
- Step 3: Apply a statistical test for all data points that are assigned to each center to find out whether these data points follow Gaussian distribution or not.
- Step 4: If there is a Gaussian distribution for s_i , keep s_i . Otherwise, replace it with two centers.
- Step 5: Repeat Step 2 while new centers are added.
- Step 6: End.

2.3. Fuzzy neighborhood DBSCAN (FN-DBSCAN) algorithm

A system based on fuzzy logic consists of three basic steps: a fuzzification step, inference step, and defuzzification step (Figure 4). In the fuzzification step, crisp inputs are converted to fuzzy inputs. After processing with the

fuzzy rules in the inference step, fuzzy outputs are obtained. These outputs are converted to crisp data in the defuzzification step. In the fuzzy approach, each element in a database belongs to all clusters with different membership degrees. Membership degrees are calculated using a membership function and get values between 0 and 1.

Fuzzy sets and subsets are the basic elements of fuzzy logic. An object is a member of each cluster with a membership degree in the fuzzy approach, in contrast to the crisp approach.

The FN-DBSCAN algorithm was developed by Nasibov and Ulutagay in 2008 [10]. They include fuzziness in the DBSCAN algorithm in order to check robustness. In Figure 4, the number of neighbors of x_1 is equal to the number of neighbors of x_2 , so the points of x_1 and x_2 are the same according to DBSCAN. However, densities of them within an ε neighborhood are different. FN-DBSCAN finds the difference between x_1 and x_2 [5, 17]. Therefore, it can be said that FN-DBSCAN is more robust. In this algorithm, ε_1 and ε_2 are input parameters.

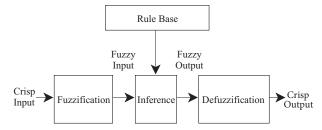


Figure 3. Structure of a fuzzy system [18].

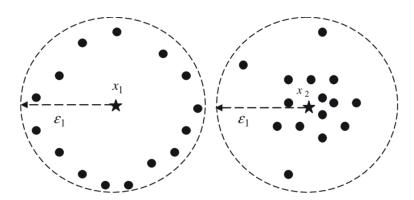


Figure 4. x_1 and x_2 points are dissimilar for fuzzy neighborhood cardinality [19].

For the *i*th point, x_i is $(x_{i1}, x_{i2}, x_{i3}, ..., x_{im})$. Here, m is the dimension of points. h is a number that takes values from 1 to m in Eq. (3). x_h^{\min} and x_h^{\max} are calculated as in Eqs. (4) and (5).

$$h = 1, ..., m \tag{3}$$

$$x_h^{\max} = \max_i x_{ih} \tag{4}$$

$$x_h^{\min} = \min_i x_{ih} \tag{5}$$

Using the values of x_h^{\min} and x_h^{\max} , the coordinates of points x_{ih} are normalized as in Eq. (6). $d(x_i^{'}, x_j^{'})$ is the distance between normalized values of x_i and x_j in Eq. (7).

$$x'_{ih} = \frac{x_{ih} - x_h^{\min}}{(x_h^{\max} - x_h^{\min})m^{1/2}}$$
 (6)

$$d(x_{i}^{'}, x_{j}^{'}) = \left(\sum_{h=1}^{m} (x_{ih}^{'} - x_{jh}^{'})^{2}\right)^{1/2}$$

$$(7)$$

First, the value of d_{max} must be calculated as in Eq. (8). There is more than one method to calculate neighborhood membership functions. There can different neighborhood membership functions used, such as Eqs. (9)–(11). The h value selected in Eqs. (10) and (11) determines the neighborhood radius, and it is greater than 0.

$$d_{\max} = \max_{i,j} (d(x_i^{'}, x_j^{'})) \tag{8}$$

$$N_{x_i}(x_j) = \left\{ \begin{array}{c} 1 - \frac{d(x_i, x_j)}{d_{\text{max}}}, ifd(x_i, x_j) \le d_0\\ 0, otherwise \end{array} \right\}$$

$$(9)$$

Here, d_0 is a given threshold value:

$$N_{x_i}(x_j) = \max\{0, 1 - h\frac{d(x_i, x_j)}{d_{\max}}\}\tag{10}$$

$$N_{x_i}(x_j) = \exp\left(-\left(h\frac{d(x_i, x_j)}{d_{\max}}\right)^2\right)$$
(11)

For each point $x_i \in D$, $N(x_i, \varepsilon_1)$ denotes the neighborhood set of the point x_i within the minimum threshold value, which is created as in Eq. (12). ω_j is the cardinality of a point j within the ε_1 in Eq. (13). ω_{max} is the maximum of $\omega_j (j = 1, ..., n)$. The input of MinPts in DBSCAN is normalized as in Eq. (14), and this value, named ε_2 , is used in the FN-DBSCAN algorithm. If any point providing Eq. (12) also provides Eq. (15), the point is a fuzzy core point.

$$N(x_i, \varepsilon_1) = \{ q \in D, N_{x_i}(q) \ge \varepsilon_1 \}$$
(12)

$$\omega_i = |N(x_i, \varepsilon_1)| \tag{13}$$

$$\varepsilon_2 = \frac{MinPts}{\omega_{\text{max}}} \tag{14}$$

$$cardFN(x; \varepsilon_1, \varepsilon_2) = \sum_{y \in N(x; \varepsilon_1)} N_x(y) \ge \varepsilon_2$$
 (15)

The FN-DBSCAN algorithm combines the advantages of the DBSCAN and NRFJP (noise-robust fuzzy joint points) algorithms and is used in many areas [19]. Its time complexity is higher than that of DBSCAN [12]. However, FN-DBSCAN is robust like NRFJP. Its algorithm is as given in Algorithm 3.

Algorithm 3. FN-DBSCAN algorithm.

- Step 1: ε_1 and ε_2 are inputs.
- Step 2: Mark all data points as unassigned. Assign 1 to t.
- Step 3: Find an unassigned fuzzy core point p with the limits of ε_1 and ε_2 . If it is not found, go to Step 9.
- Step 4: Assign p to a new cluster C_t and mark it as assigned.
- Step 5: Create a set of S and put all ε_1 neighbors to the p points, which are not assigned yet, into S.
- Step 6: Get an unassigned point q, which is in S. Assign q to C_t . Remove q from S and mark it as assigned.
- Step 7: If q is a fuzzy core point, add all unassigned points in the ε_1 neighborhood of q to S.
- Step 8: Repeat Steps 6 and 7 if S is not an empty set.
- Step 9: Increase t=t+1 and go to Step 3.
- Step 9: If there is an unassigned point, assign it as noise.
- Step 10: End.

2.4. The proposed algorithm: FN-DBSCAN-GM

The FN-DBSCAN-GM algorithm is the combination of fuzziness, the DBSCAN algorithm, and the Gaussian means (G-means) algorithm. DBSCAN, the fuzzy version of DBSCAN (FN-DBSCAN), and the G-means algorithms were mentioned above. FN-DBSCAN-GM takes advantages of them. It benefits from FN-DBSCAN for robustness, and from G-means to avoid the need for inputs. First, each point is normalized using Eq. (6). All distances between points are calculated as in Eq. (7). If there is no information about the number of clusters, the number of clusters, which is called k, starts with 1 (otherwise, k starts from the known number). To find the correct value of k and to obtain optimal clustering, the Gaussian means algorithm is run. If there is a Gaussian distribution, the right number for the data is reached and the K-means algorithm is run again. r_j is the radius of cluster j, and it is estimated with Eq. (16). The global ε_1 is the minimum element of radii. After that, total volumes for each center are calculated as in Eq. (17). Then ε_{2i} values are calculated in Eq. (18). The ε_{2i} value is the local ε_2 value for the cluster i. The global ε_2 is the smallest ε_{2j} by Eq. (19). The FN-DBSCAN code is now tested because parameters that it needs are found. The algorithm of FN-DBSCAN-GM is as given in Algorithm 4.

$$r_j = \sqrt{\frac{\sum_{i=1}^n d(c_j, x_{ij})^2}{n_j}}, j = 1, 2, \dots$$
 (16)

$$V_j = \frac{4}{3} \Pi r_j^3, j = 1, 2, \dots$$
 (17)

$$\varepsilon_{2j} = \frac{\frac{\Pi r_j^2 n_j}{V_j}}{\omega_{\text{max}}}, j = 1, 2, \dots$$
(18)

$$\varepsilon_2 = \min_j \varepsilon_{2j} \tag{19}$$

The time complexity of FN-DBSCAN-GM should be mentioned. The algorithm runs a number of instructions. n is the number of objects. K is the number of clusters. I is the number of iterations and d is the number of attributes. The time complexity of the K-means algorithm is O(nKId). The time complexity of checking a Gaussian distribution for all data points is O(n). The time complexity of the FN-DBSCAN algorithm is $O(n^2)$. Finally, the time complexity of the proposed algorithm is $O(nKId) + O(n) + O(n^2) = \max\{O(n^2), O(nKId)\}$. In general, the time complexity of the proposed algorithm will be approximately $O(n^2)$ because $n \gg KId$.

Algorithm 4. FN-DBSCAN-GM algorithm.

Step 1: $S = \{s_i\}$ is the set of centers.

Step 2: Apply the K-means algorithm for an initial set of centers.

Step 3: Apply a statistical test for all data points assigned to s_i to figure out whether the data points follow a Gaussian distribution or not.

Step 4: If there is a Gaussian distribution for si, keep si. Otherwise replace si with two centers.

Step 5: Repeat Step 2 until a new center is added.

Step 6: Calculate

 $\varepsilon_1 = min\{r_i|for\ all\ s_i \in S\}$

and

 ε_2 according to Eq. (19).

Step 7: Mark all points as unassigned. Set t=1.

Step 8: Find a fuzzy core point p, which is unassigned and provides the limits of ε_1 and ε_2 . If it is not found, go to Step 15.

Step 9: Assign p to a new cluster C_t and mark it as assigned.

Step 10: Create a set of S and put all ε_1 neighbors to the p points, which are not assigned yet, into S.

Step 11: Get an unassigned point q, which is in S. Assign q to C_t . Remove q from S and mark it as assigned.

Step 12: If q is a fuzzy core point, add all unassigned points in the ε_1 neighborhood of q to S.

Step 13: Repeat Steps 11 and 12 if S is not an empty set.

Step 14: Increase t=t+1 and go to Step 8.

Step 15: If there is an unassigned point, assign it as noise.

Step 16: End.

3. Experimental results

A comparison among the K-means, G-means, DBSCAN, DBSCAN-GM, and FN-DBSCAN-GM algorithms is made in this section. Algorithms were implemented in MATLAB.

In cluster analysis, most close elements are in the same cluster, and dissimilar elements are in different clusters. Discovering interesting relationships for datasets and determining the patterns are adjusted in this way. There are several methods in the literature for clustering. When different methods are applied, datasets can be split into different clusters even if the number of clusters is the same. Cluster validity indices are used for evaluating the quality of the clustering, measuring the performance, and finding the correct number of clusters. In this study, algorithms were compared using the validity index of Eq. (20). k is the number of clusters. $center_i$ is the center of cluster C_i . n is the number of data points. i gets integer values between 1 and k-1. j gets values between the interval [i+1,k]. In the equation, the minimum of two different centers is used.

$$Validity = \frac{\frac{1}{n} \sum_{i=1}^{k-1} \sum_{x \in C_i} (x - center_i)}{\min_{i,j} (center_i - center_j)}$$
(20)

Using a percentage of correct classification (PCC), the algorithms were analyzed. To compare FN-DBSCAN-GM with the other clustering algorithms, six artificial and two real datasets found on the Internet were used. There is some information about the used artificial datasets (sizes and number of clusters) in this study in Table 1. The FN-DBSCAN-GM algorithm finds clusters with one hundred percent accuracy for all of the artificial datasets and it is successful for real-life datasets as in Table 2. While DBSCAN is successful for most of the data, K-means was not found to be successful for these datasets.

Smiti and Elouedi compared DBSCAN-GM with K-means, G-means, and DBSCAN [8,9]. They measured the performance of the algorithms using PCC and the validity index above. We compared the results they obtained from these tests with the results we obtained from the method we developed.

There are results of experiments on real-life datasets (Iris, Indian) in Tables 3 and 4. The Iris dataset has 150 flower data. Each object in the Iris dataset has four attributes. The Indian dataset has 768 data. The number of attributes in the Indian dataset is nine. As can be seen from the Table 3, PCC values of the FN-DBSCAN-GM algorithm are greater than the others.

Datasets	Size	Cluster number	
Spiral-1	200×2	2	
Wave	287×2	2	
Spiral-2	312×2	3	
Face	320×2	4	
Moon	514×2	4	
Ring	800 × 2	2	

Table 1. The properties of artificial datasets.

Table 2. PCC values of artificial datasets.

Datasets	K-MEANS	DBSCAN	FN-DBSCAN-GM
Spiral-1	43.5	100	100
Wave	73.519	100	100
Spiral-2	54.915	78	100
Face	86.5625	100	100
Moon	65.078	100	100
Ring	46	100	100

Table 3. PCC values of Iris and Indian datasets.

Datasets	K-MEANS	G-MEANS	DBSCAN	DBSCAN-GM	FN-DBSCAN-GM
Iris	95.270	97.67	98.33	98.55	98.59
Indian	8.150	2.583	97.6	99	99.82

Table 4. Validity values of Iris and Indian datasets.

Datasets	K-MEANS	G-MEANS	DBSCAN	DBSCAN-GM	FN-DBSCAN-GM
Iris	1.483	0.272	0.33	0.261	0.0667
Indian	3.171	3.431	1.914	2.198	0.0022

Figures 5–7 show outputs obtained from the artificial datasets. Columns a and b indicate the results from different datasets. Parameters that provide better results were entered for the DBSCAN algorithm and the number of clusters was entered for the K-means algorithm. The quality of FN-DBSCAN-GM is understood specifically from the datasets of Spiral-2 and Moon. It finds overlapping clusters effectively.

The comparison of time complexities is given in Table 5. The time complexity of the FN-DBSCAN-GM algorithm is approximately $O(n^2)$.

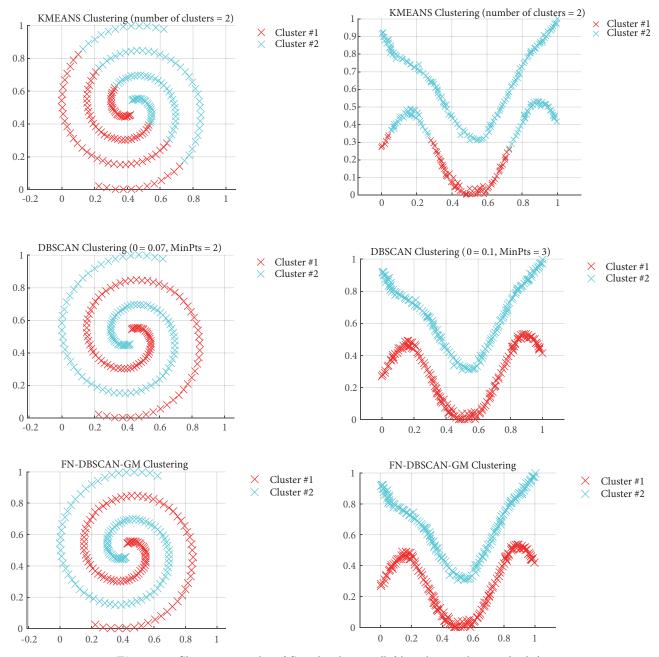


Figure 5. Clustering results of Spiral-1 dataset (left) and wave dataset (right).

Results of the FN-DBSCAN and DBSCAN algorithms are compared by changing the values of input parameters. When input parameters give the correct results in the FN-DBSCAN and DBSCAN algorithms, the reached result is 170 (ε_1 , ε_2) optimal input parameters for the FN-DBSCAN algorithm and 94 (ε , MinPts) optimal input parameters for the DBSCAN algorithm. MinPts is the minimum number of points in the ε neighborhood of a core point. Therefore, the value of MinPts must be an integer number. ε_1 , ε_2 , and ε can take decimal values. Tests were continued by increasing the values of ε , ε_1 , and ε_2 by 0.01, within the interval [0,1]. The number of parameters that give correct results for the FN-DBSCAN algorithm is greater than the number of parameters that give correct results for the DBSCAN algorithm. According to this result, it can be

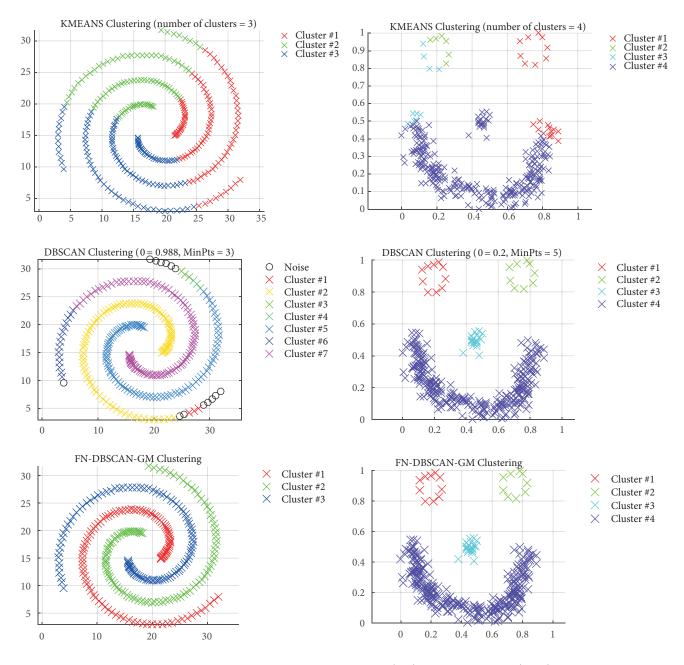


Figure 6. Clustering results of Spiral-2 dataset (left) and Face dataset (right).

inferred that the probability of finding the right parameters of the FN-DBSCAN-GM algorithm is greater than the probability of finding the right parameters of DBSCAN-GM. Therefore, the FN-DBSCAN-GM algorithm is more robust than the DBSCAN-GM algorithm.

4. Conclusion

A new clustering algorithm, FN-DBSCAN-GM, which is based on densities, is proposed in this study. Tests were done on six artificial datasets and two real-life datasets. The newly developed algorithm was successful in finding the parameters of the DBSCAN algorithm, and also it gave more robust results than the DBSCAN

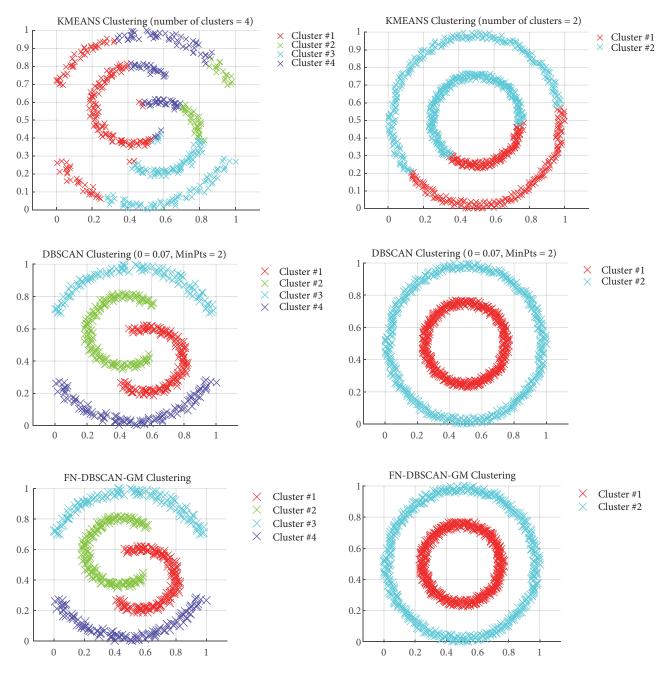


Figure 7. Clustering results of Moon dataset (left) and Ring dataset (right).

algorithm and the DBSCAN-GM algorithm. Compared to the other clustering algorithms (K-means, G-means, DBSCAN, DBSCAN-GM), the FN-DBSCAN-GM algorithm discovers all clusters for both artificial and real-life datasets. According to test results, the proposed FN-DBSCAN-GM algorithm can be preferred in different areas for datasets in areas using fuzzy neighborhood relations (data mining, pattern processing, fabric error detection, etc.).

FN-DBSCAN-GM has many advantages. However, the time complexity is not good enough, especially for big data. The time complexity of FN-DBSCAN-GM will be reduced as future work.

Method	Time complexity
K-means	O(nKId)
DBSCAN	O(nlogn)
DBSCAN-GM	3. O(nlogn)
FN-DBSCAN	$O(n^2)$
FN-DBSCAN-GM	$O(n^2)$

Table 5. Time comparisons.

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